Numerical approaches for Painlevé equations

We discuss numerical approaches for Painlevé equations based on standard ODE methods for boundary value problems: the equations are discretised via a collocation method offering spectral convergence, and the resulting system is solved iteratively with a Newton method. The boundary data are obtained via a truncated asymptotic series or via compactification techniques. Several examples are discussed.