

The Large-Misalignment Mechanism for the Formation of Compact Axion Structures

Ken Van Tilburg (KITP)

A. Arvanitaki, S. Dimopoulos, M. Galanis, L. Lehner, J. Thompson, KVT:
[arXiv:1909.11665](https://arxiv.org/abs/1909.11665)

“Problems” in particle physics

Standard Model of particle physics accurately describes every known experiment and observation to the measured and calculated precision*

theoretical frontiers:

mathematical structures | parametric curiosities | computational precision

experimental frontiers:

high-energy | cosmic | intensity | precision

***parametrized unknowns:**

dark matter | baryon asymmetry | inflation

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[production] *[initial conditions]*

The *Large-Misalignment Mechanism* for the Formation of *Compact Axion Structures*

Large Misalignment for Compact Axion Structures

Axions behave exactly like Cold Dark Matter (CDM)*

*except under **certain conditions**, on some **length scales**, and at **times** when they do not

Symmetry breaking after inflation: isocurvature fluctuations \rightarrow axion strings & miniclusters

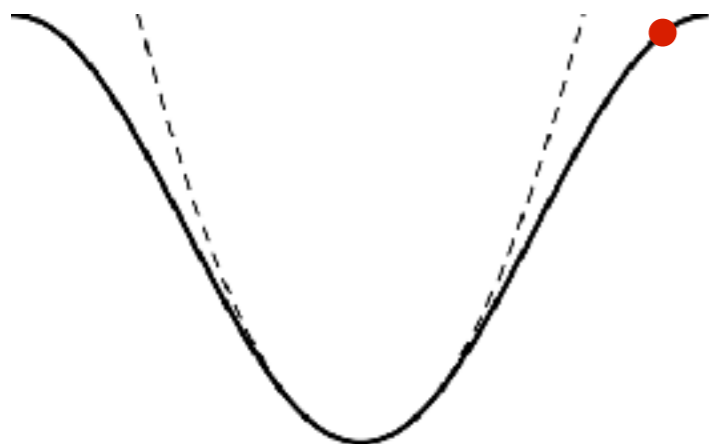
Symmetry breaking before inflation, small misalignment: density fluctuations suppressed below Jeans scale

Symmetry breaking before inflation, large misalignment:

density fluctuations enhanced for **semi-relativistic modes** when the axion starts oscillating

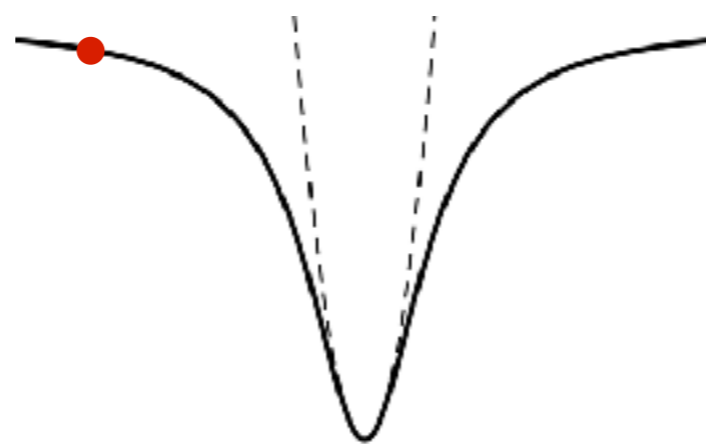
cosine

$$V = -m^2 f^2 \cos \frac{\phi}{f}$$



modulus

$$V = \frac{m^2 f^2}{2} \frac{\phi^2}{f^2 + \phi^2}$$



QCD axion

$$V = -m_a(T)^2 f_a^2 \cos \frac{a}{f_a}$$



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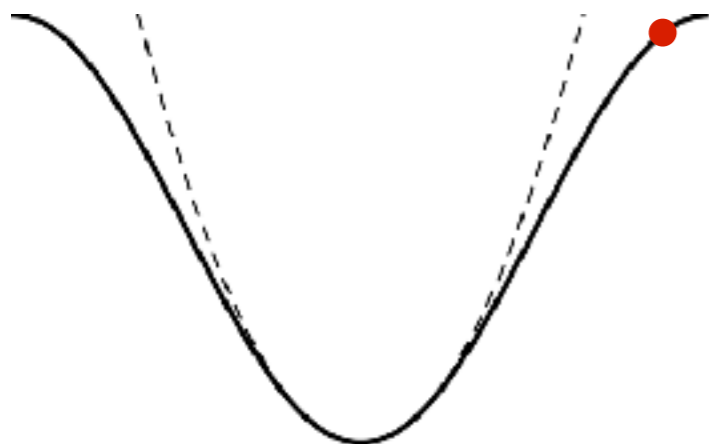
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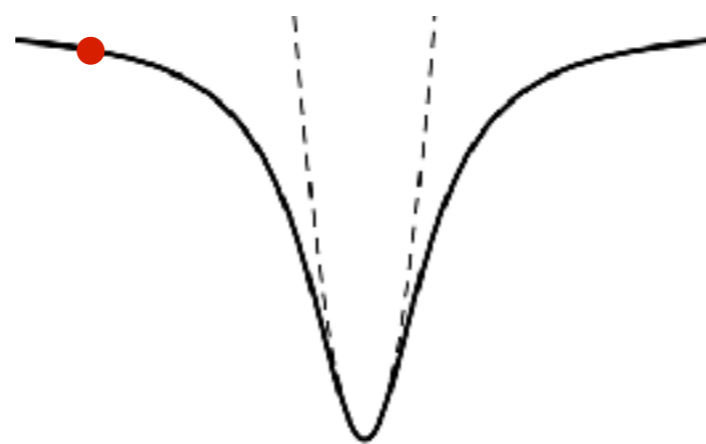
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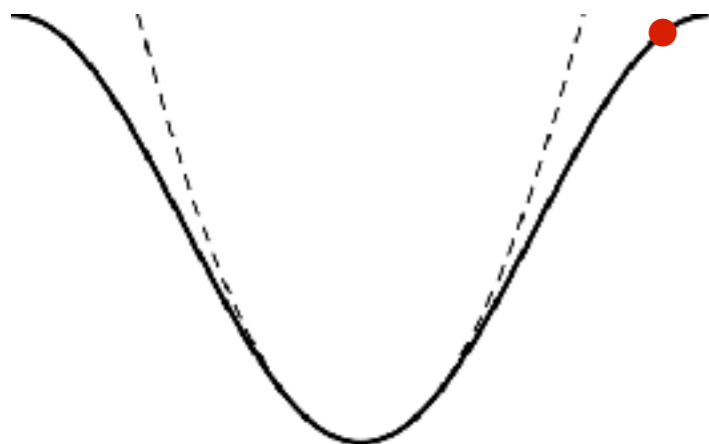
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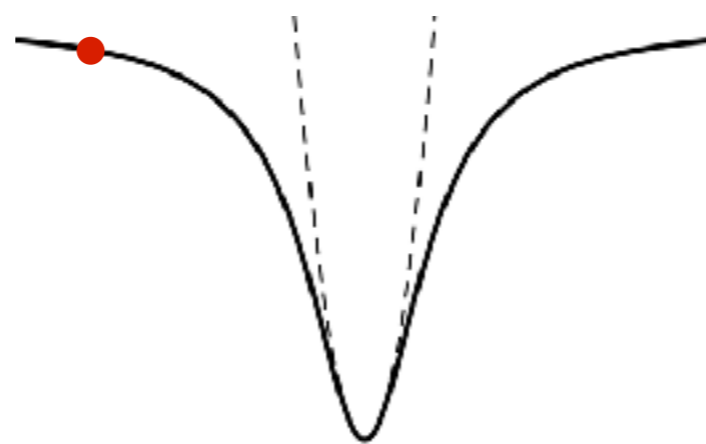
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QCD axion

$$V = -m_\pi^2 f_\pi^2 \sqrt{1 - \frac{4m_u m_d}{(m_u + m_d)^2} \sin^2 \left(\frac{a}{2f_a} \right)}$$



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$$\text{if } |\Theta_0| > \frac{\pi}{2} : \quad \text{for } \frac{k}{a} \sim m \sim H_{\text{osc}}$$

$$\mathcal{B} \equiv \frac{\rho_s}{\rho_s^{\text{CDM}}} \sim \exp \left\{ \frac{m}{H_{\text{osc}}} \right\} \quad M_s^* \sim \frac{\rho_{\text{DM}}^0}{(k_*)^3} \sim 5 \times 10^9 M_\odot \left[\frac{10^{-22} \text{ eV}}{m} \right]^{3/2}$$

Large Misalignment Mechanism

$$\frac{\phi}{f} = \Theta(t) + \sum_{\mathbf{k}} \theta_{\mathbf{k}}(t) e^{i\mathbf{k}\cdot\mathbf{x}} \quad \tilde{k}^2 \equiv \frac{k^2/a^2}{2mH}$$

3 ways to understand enhancement of structure formation:

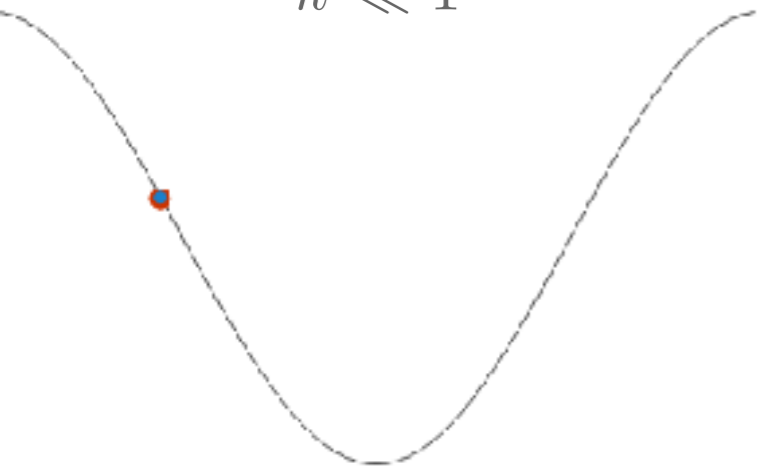
1. negative quartic \rightarrow attractive self-interaction $V = m^2 f^2 [1 - \cos \theta] \simeq m^2 f^2 \left[\frac{\theta^2}{2} - \frac{\theta^4}{24} + \dots \right]$

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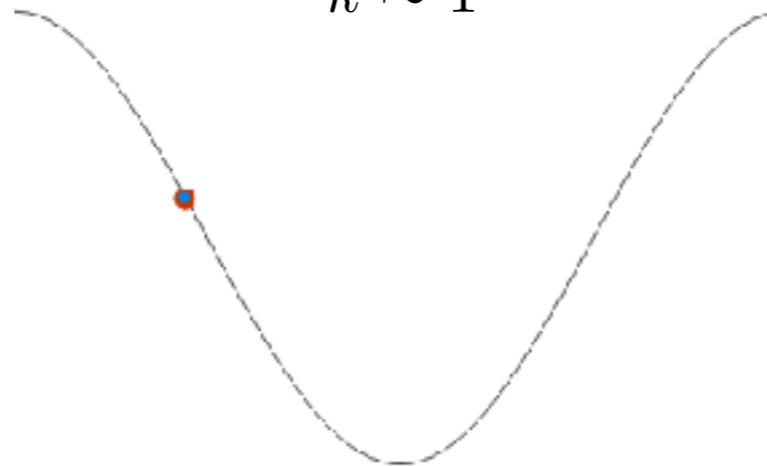
3. parametric resonance for field fluctuations

nonrelativistic mode
 $\tilde{k} \ll 1$



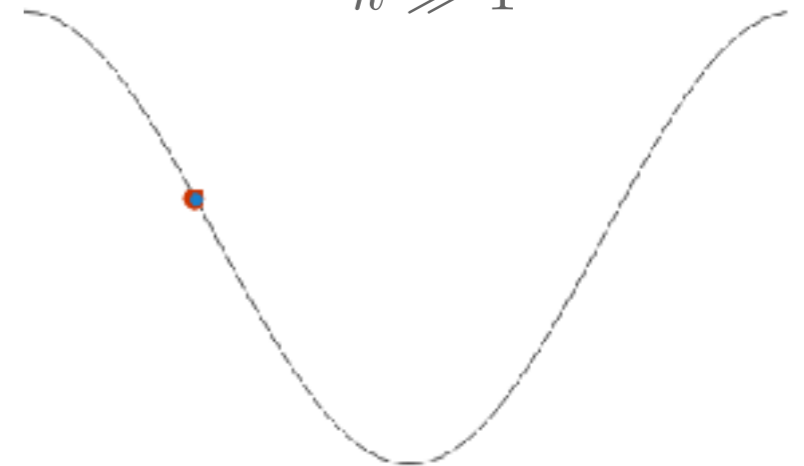
enters horizon when nonlinearities are small

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frequency match; nonlinearity > friction

ultra-relativistic mode
 $\tilde{k} \gg 1$



frequency mismatch; curvature fluctuation damped

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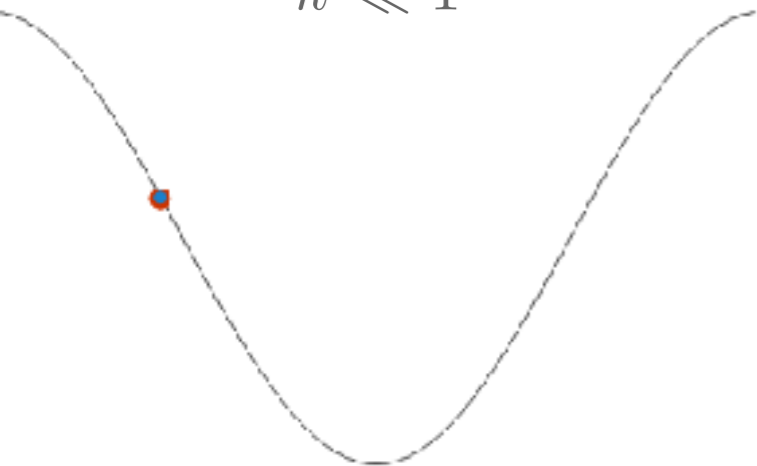
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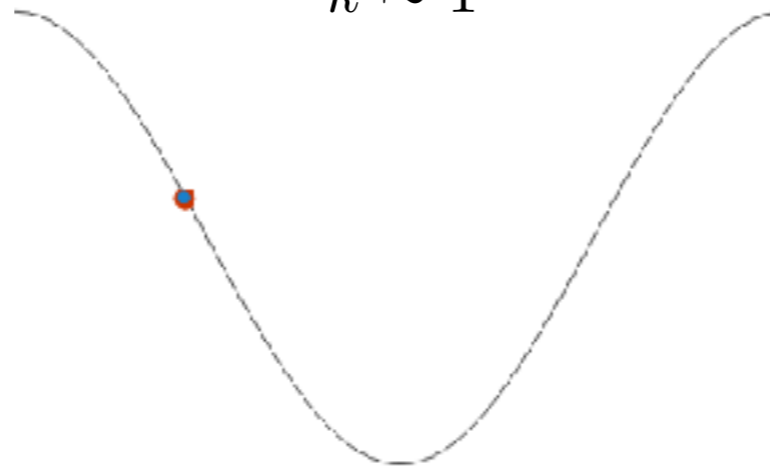
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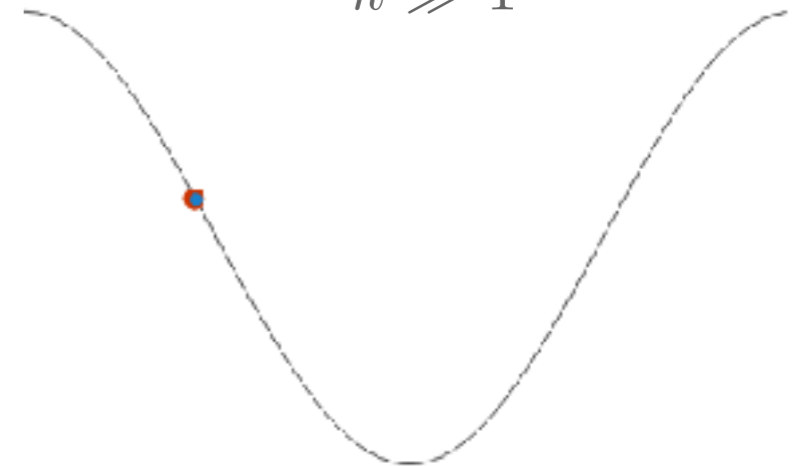
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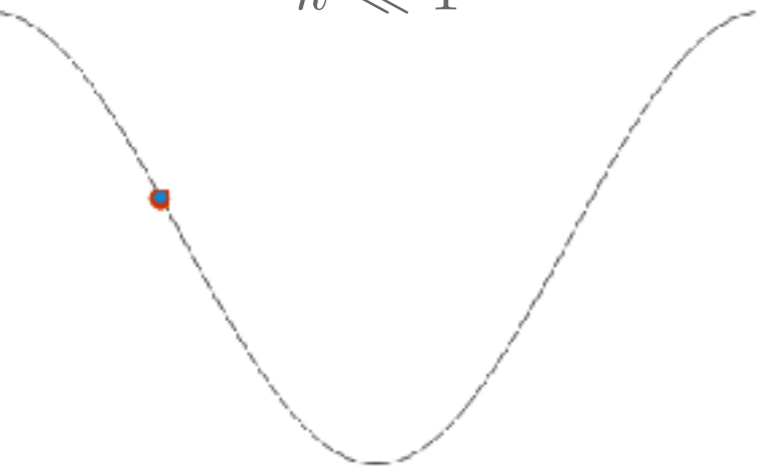
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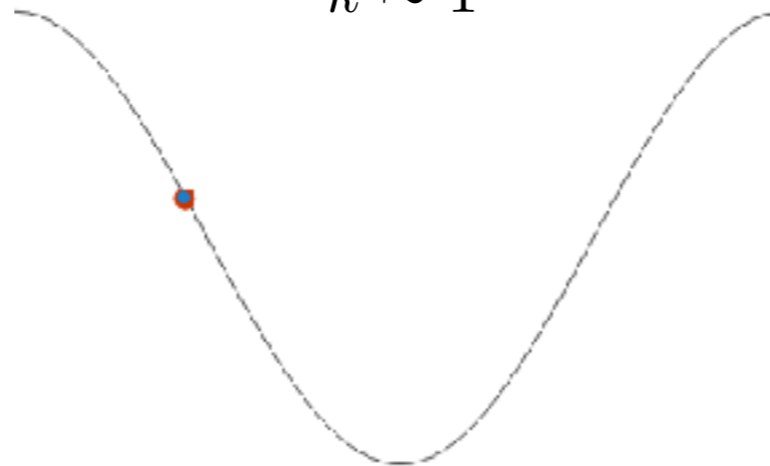
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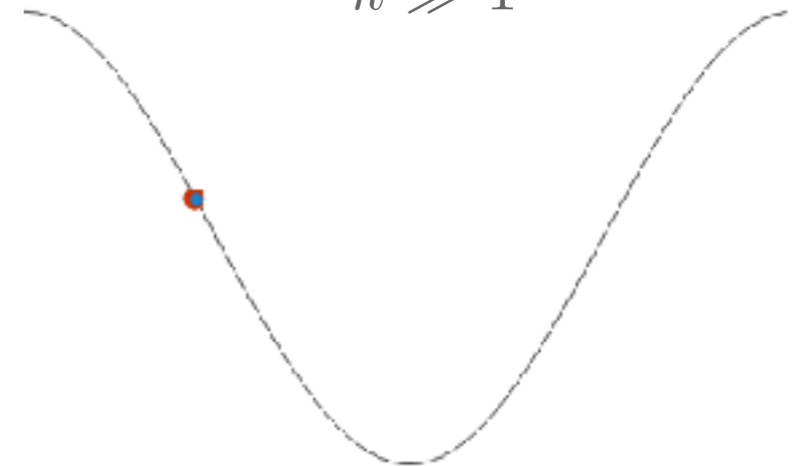
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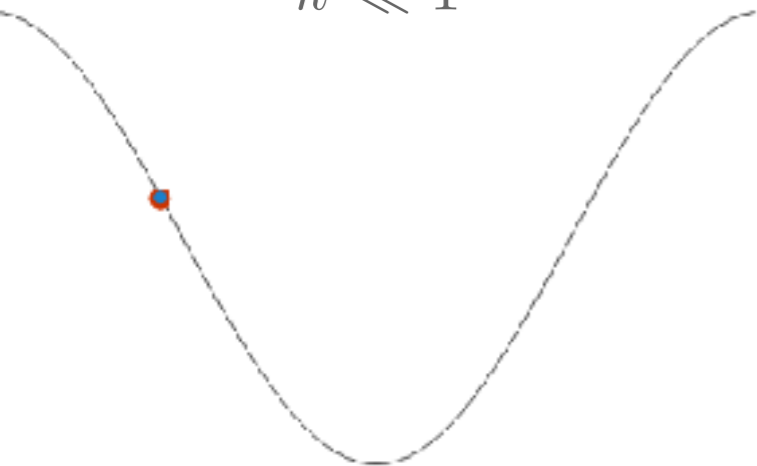
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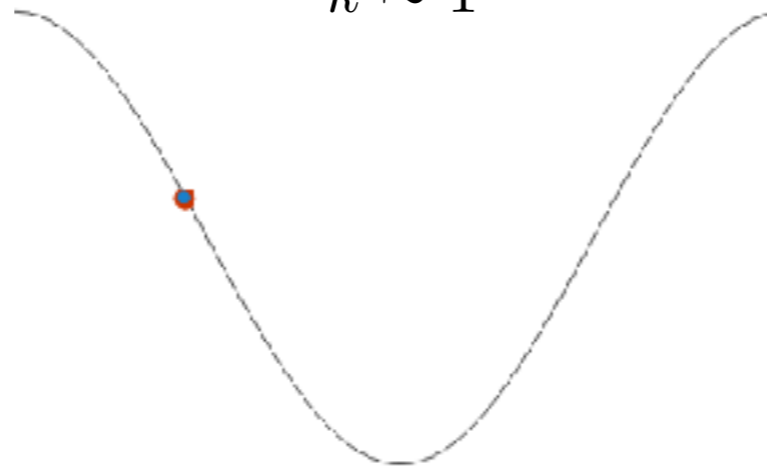
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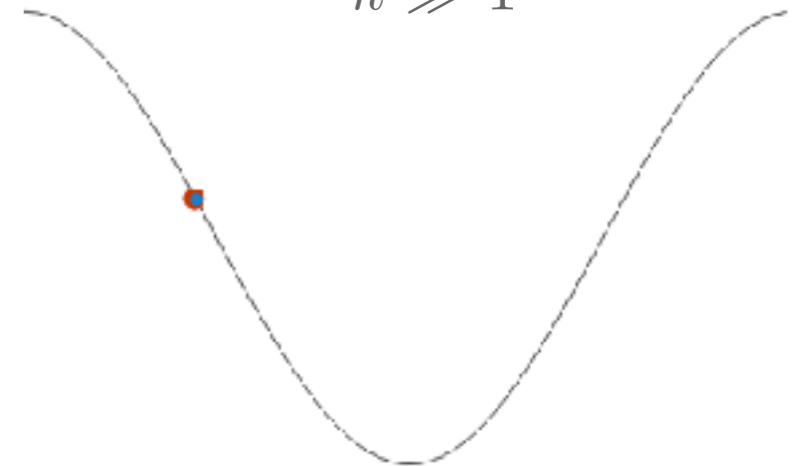
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Compact Axion Structures

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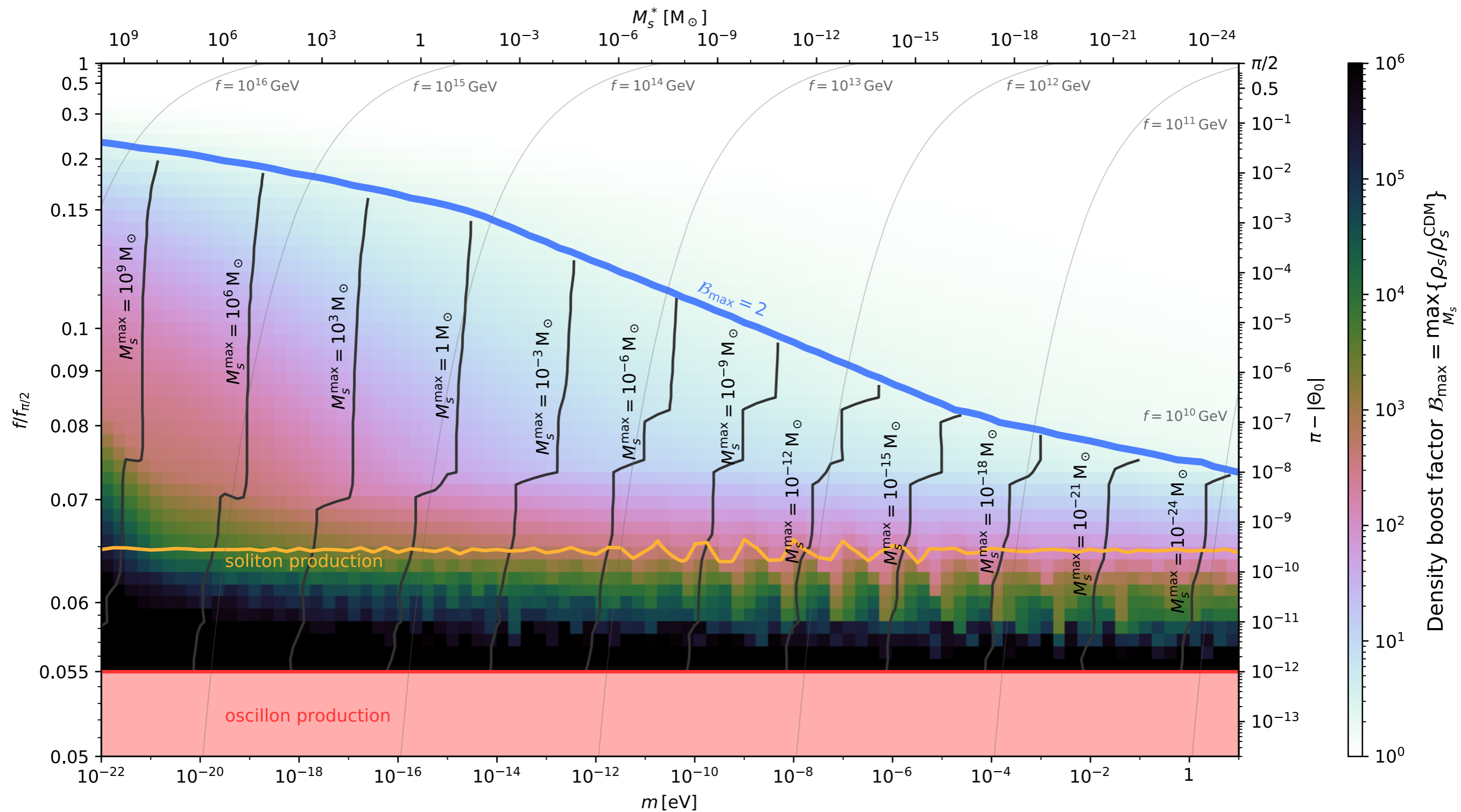
dense axion minihalos

solitons

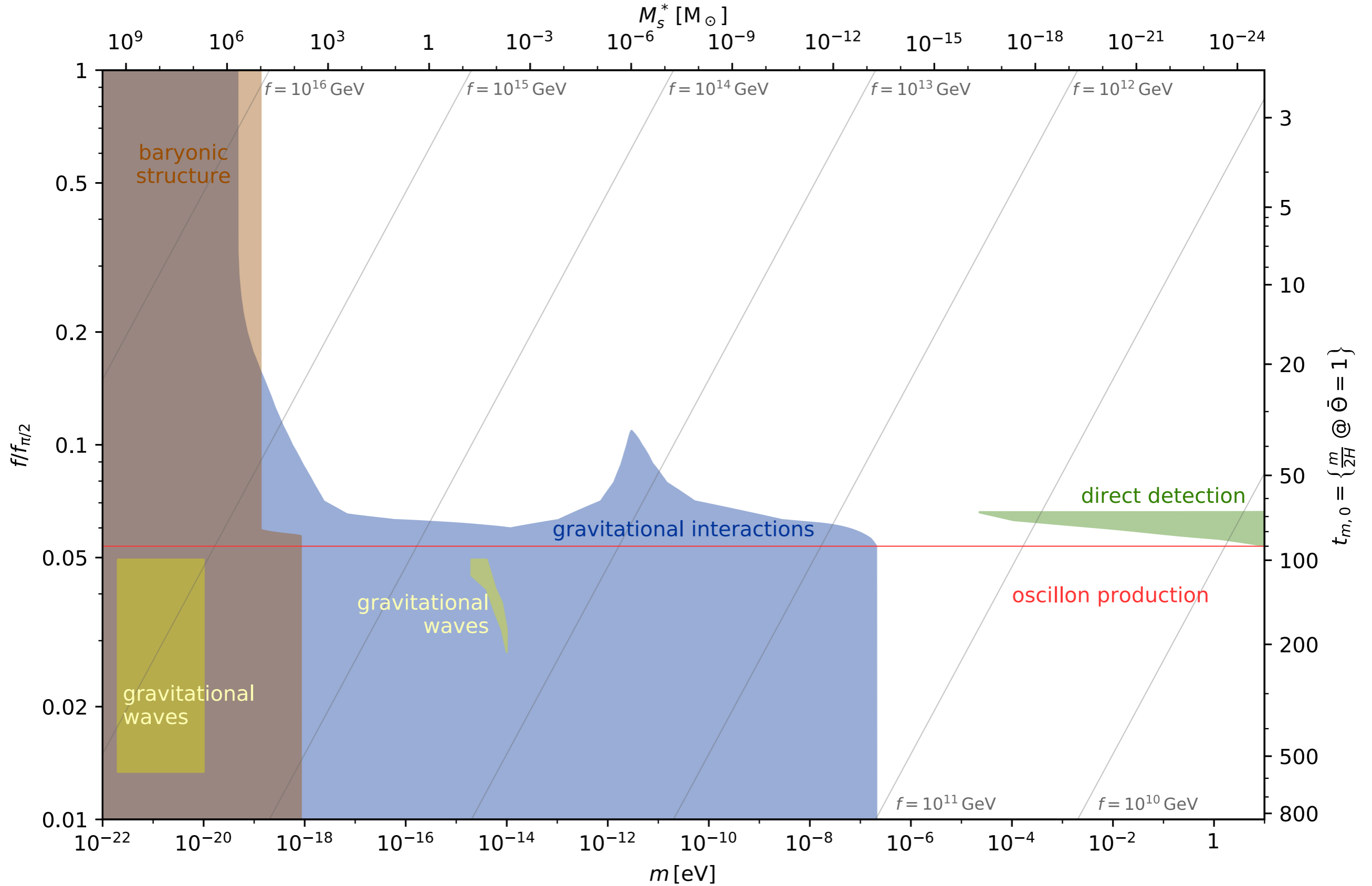
oscillons

[gravity+kinetic]

[self-interactions+kinetic]



Observable Signatures



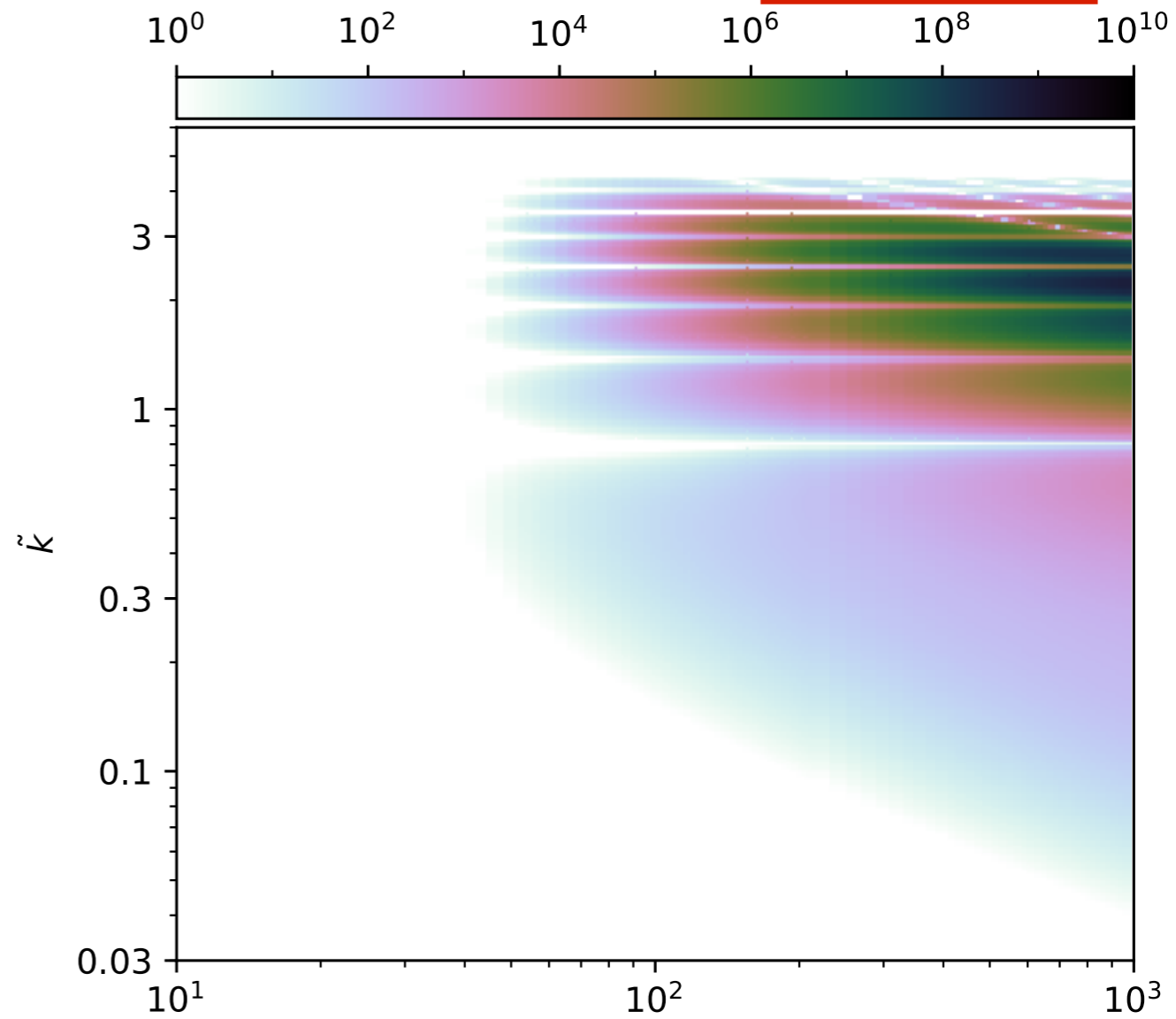
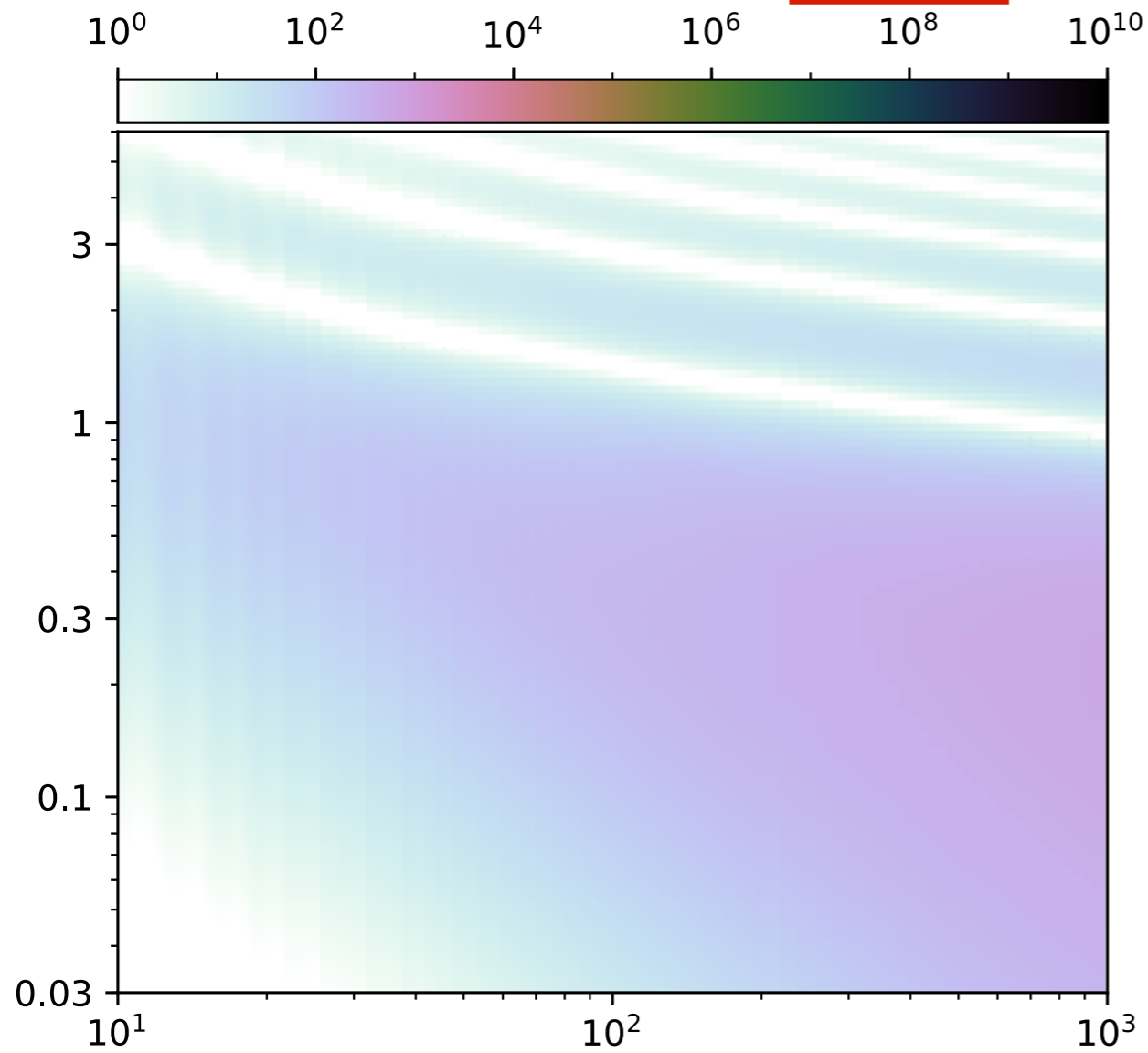
Linear Evolution in Time

small misalignment

large misalignment

Transfer Function $|\delta_k/\Phi_0|^2$, $|\Theta_0| = 0.1$

Transfer Function $|\delta_k/\Phi_0|^2$, $\pi - |\Theta_0| = 10^{-10}$



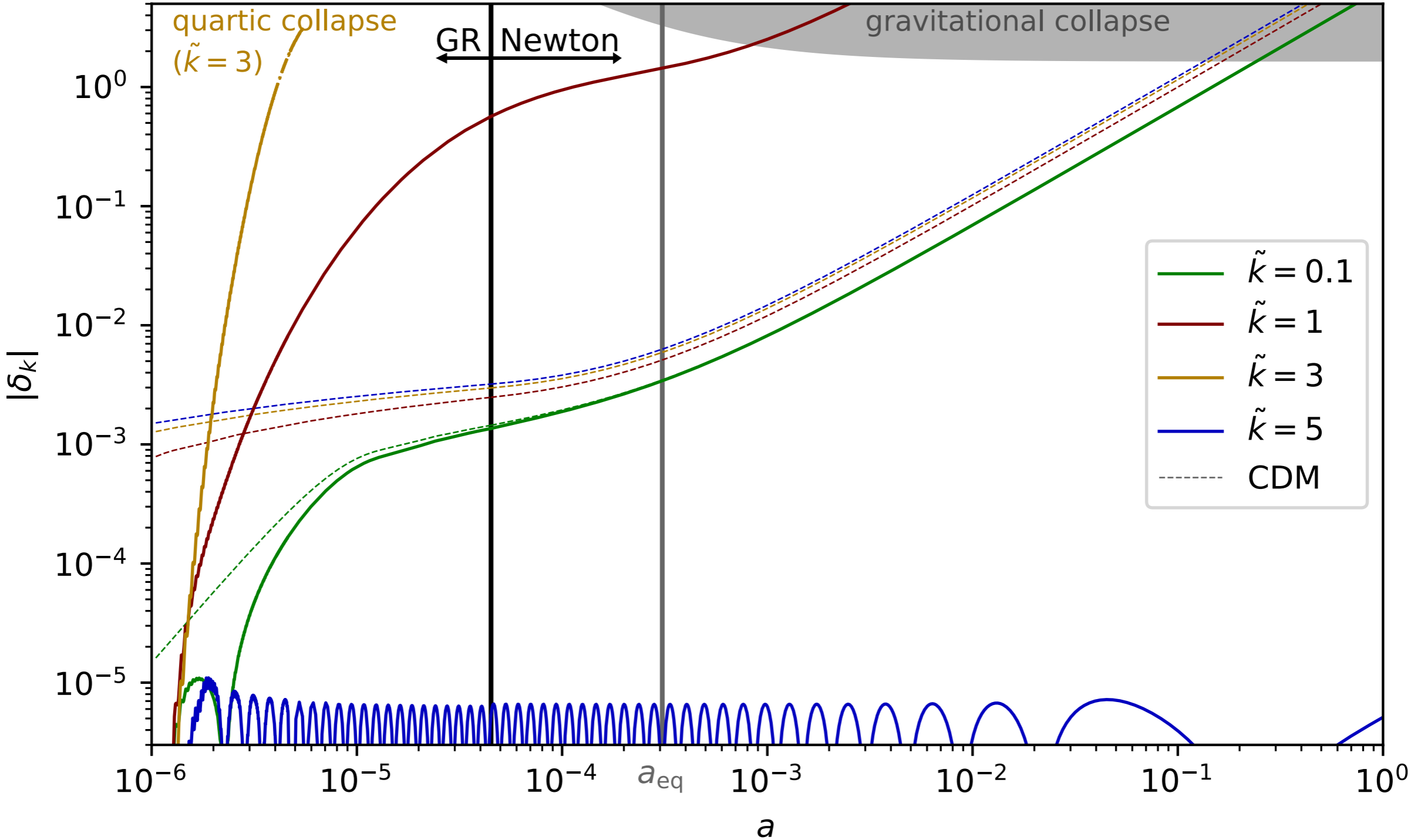
t_m

t_m

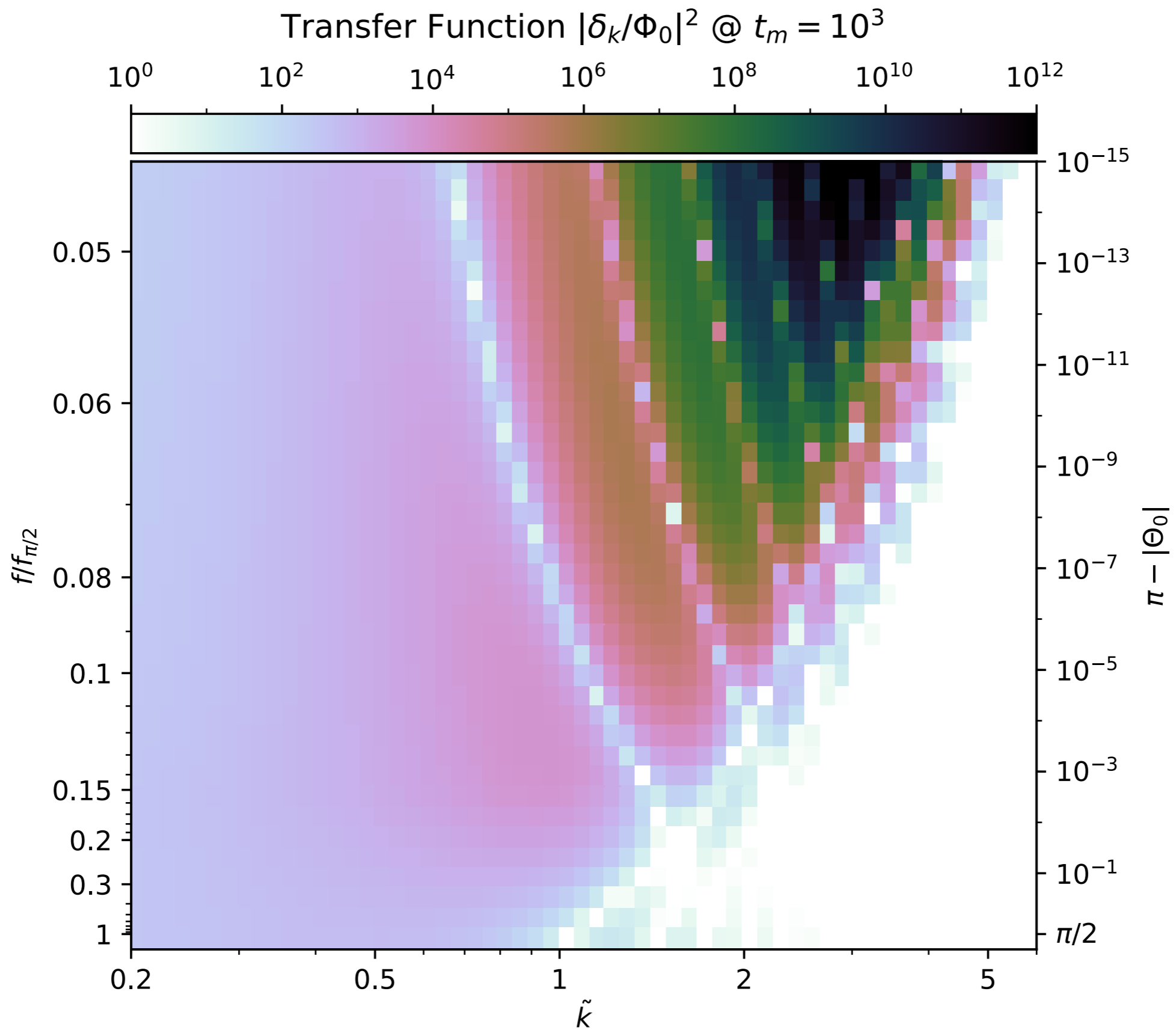
time in Compton units

Linear Evolution in Time

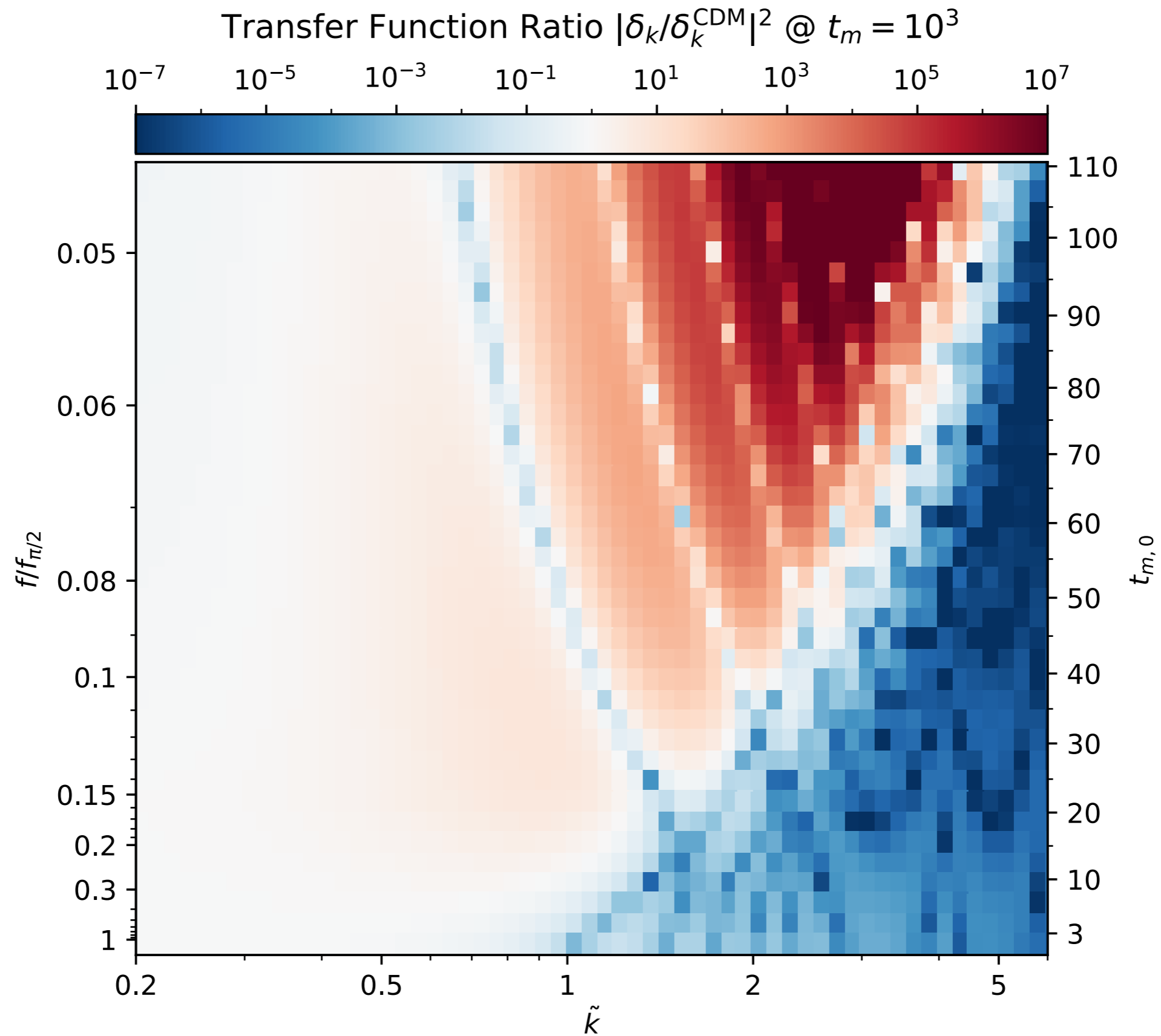
$$m = 10^{-21} \text{ eV}; \quad \pi - |\Theta_0| = 10^{-12}; \quad \Phi_0^2 = 2.1 \times 10^{-9}$$



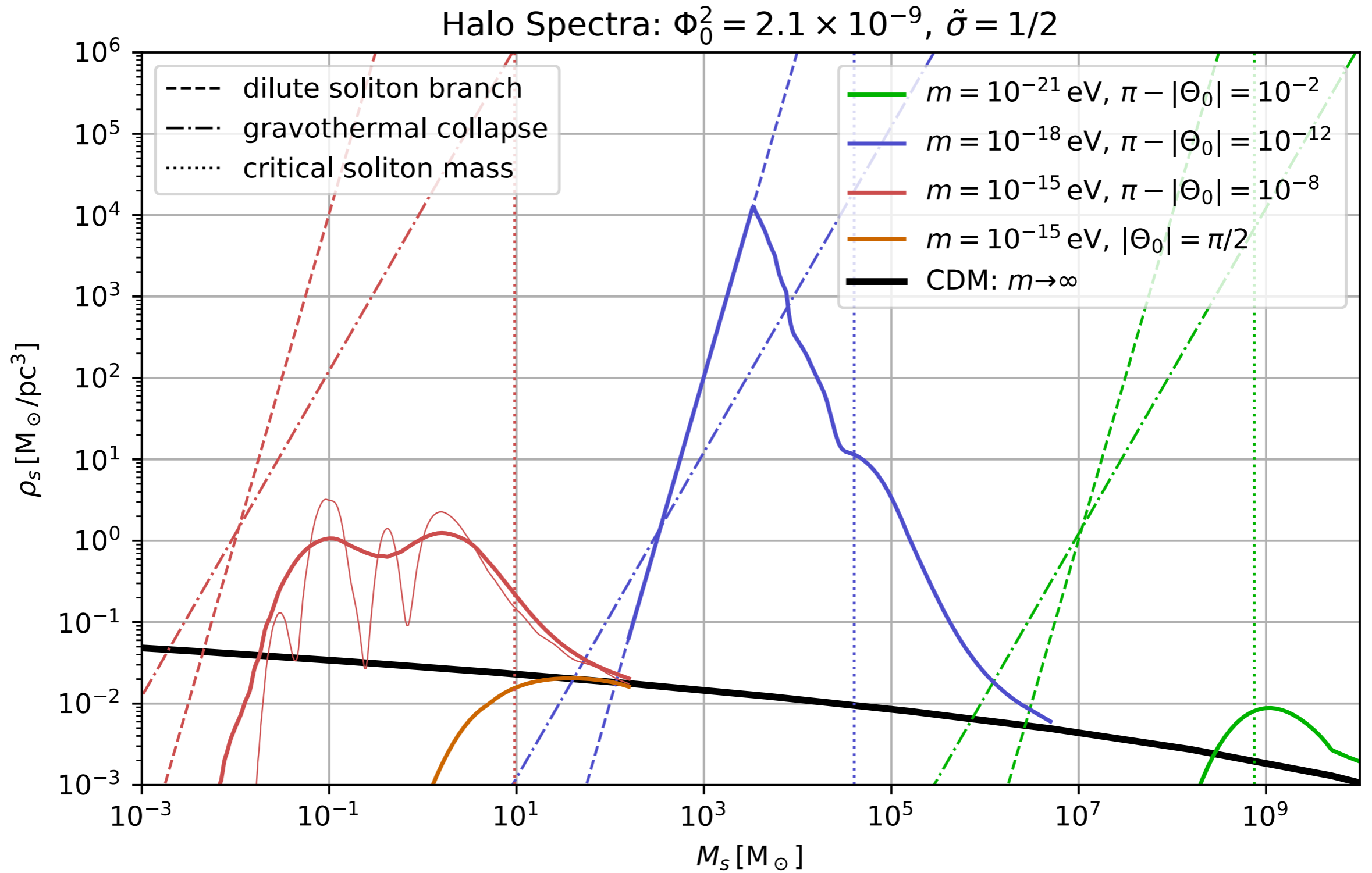
Linear Evolution versus Misalignment



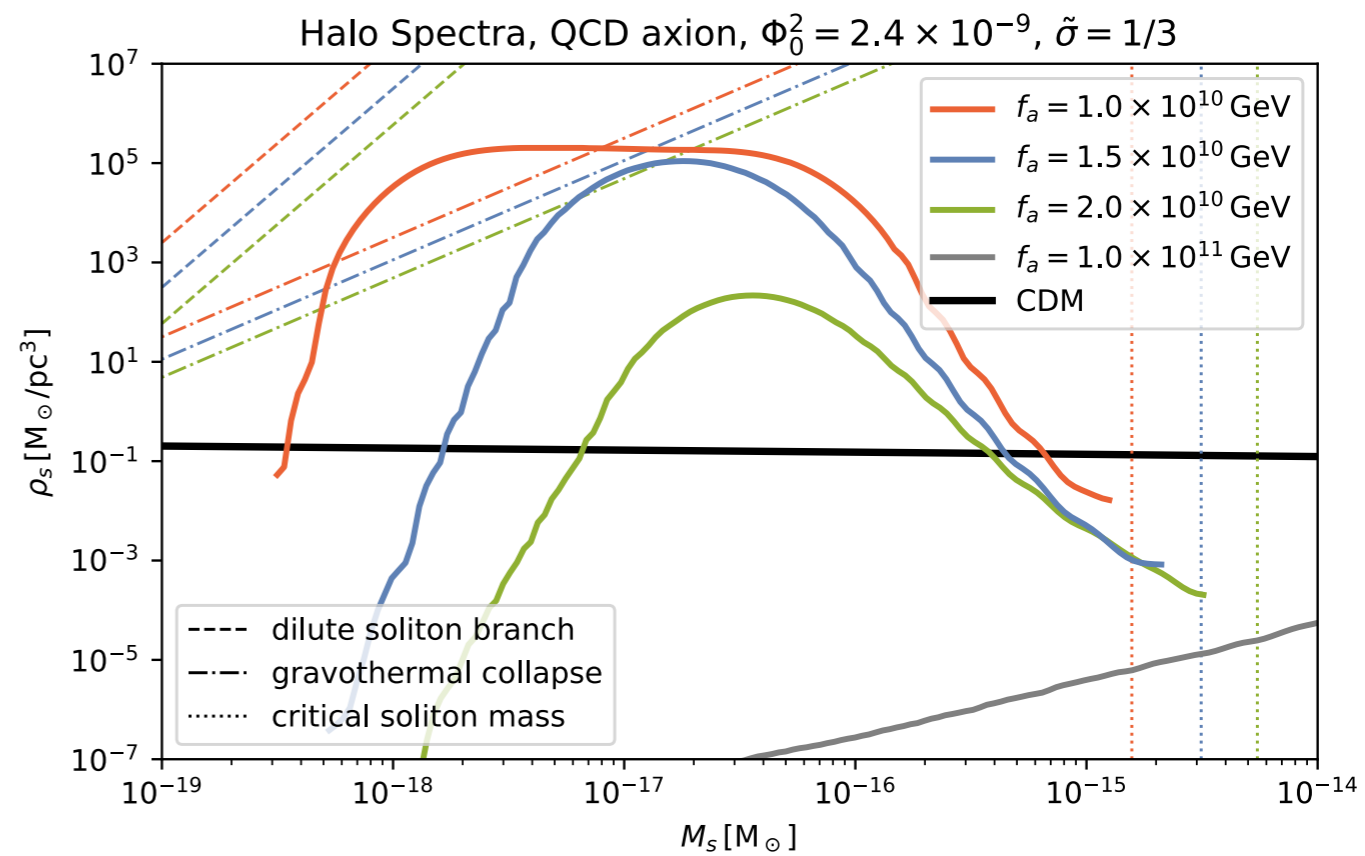
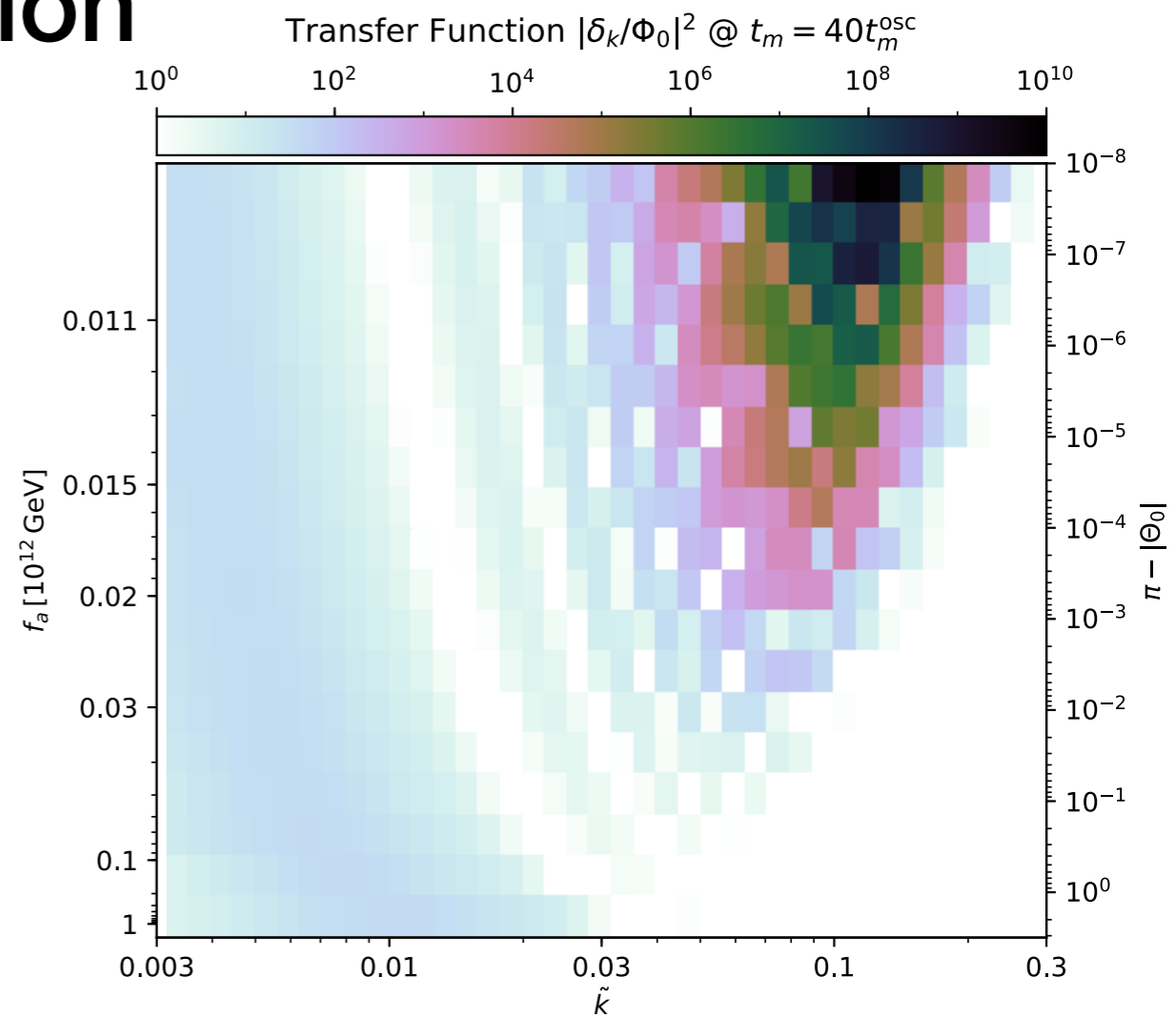
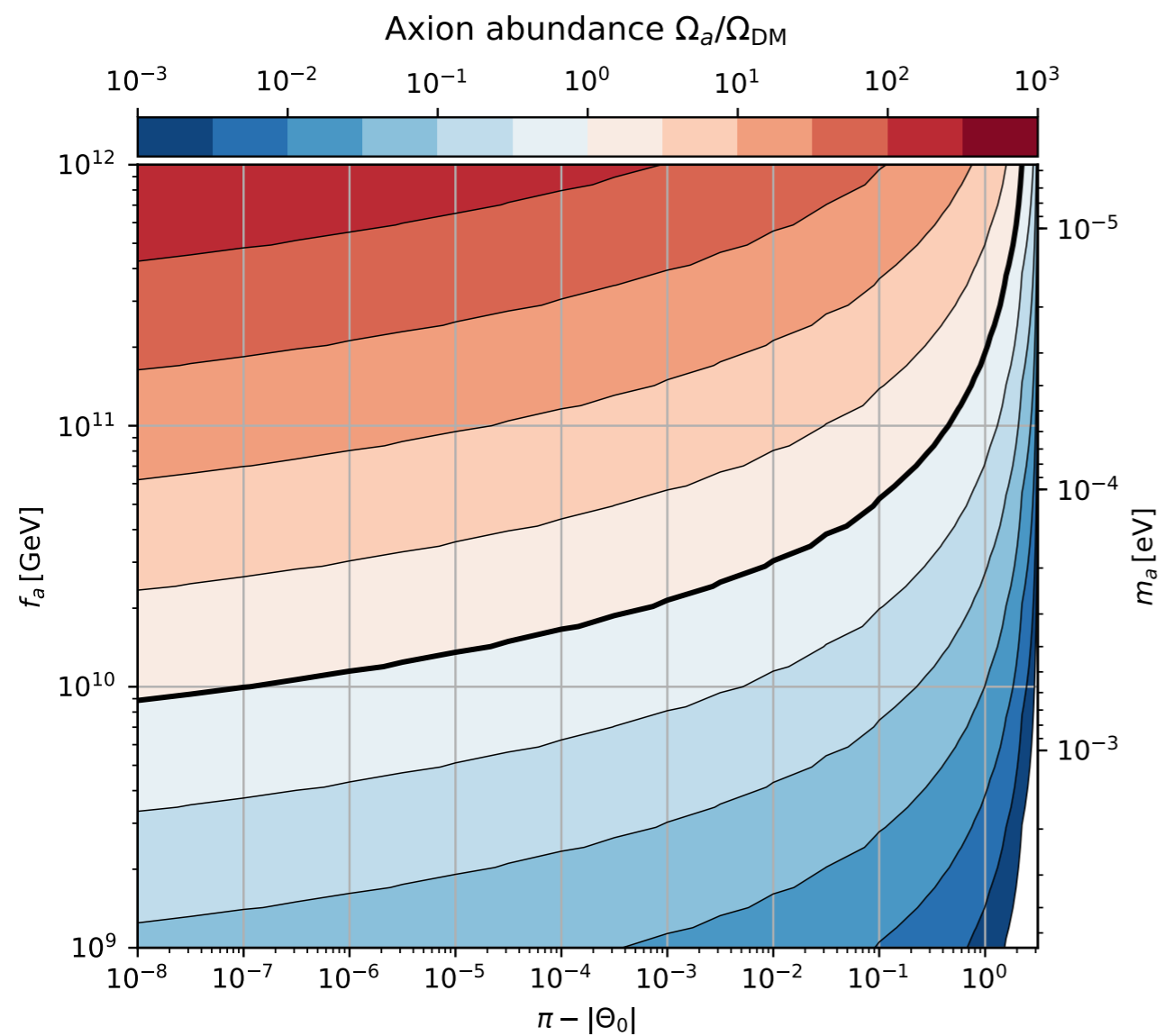
Linear Evolution versus Misalignment



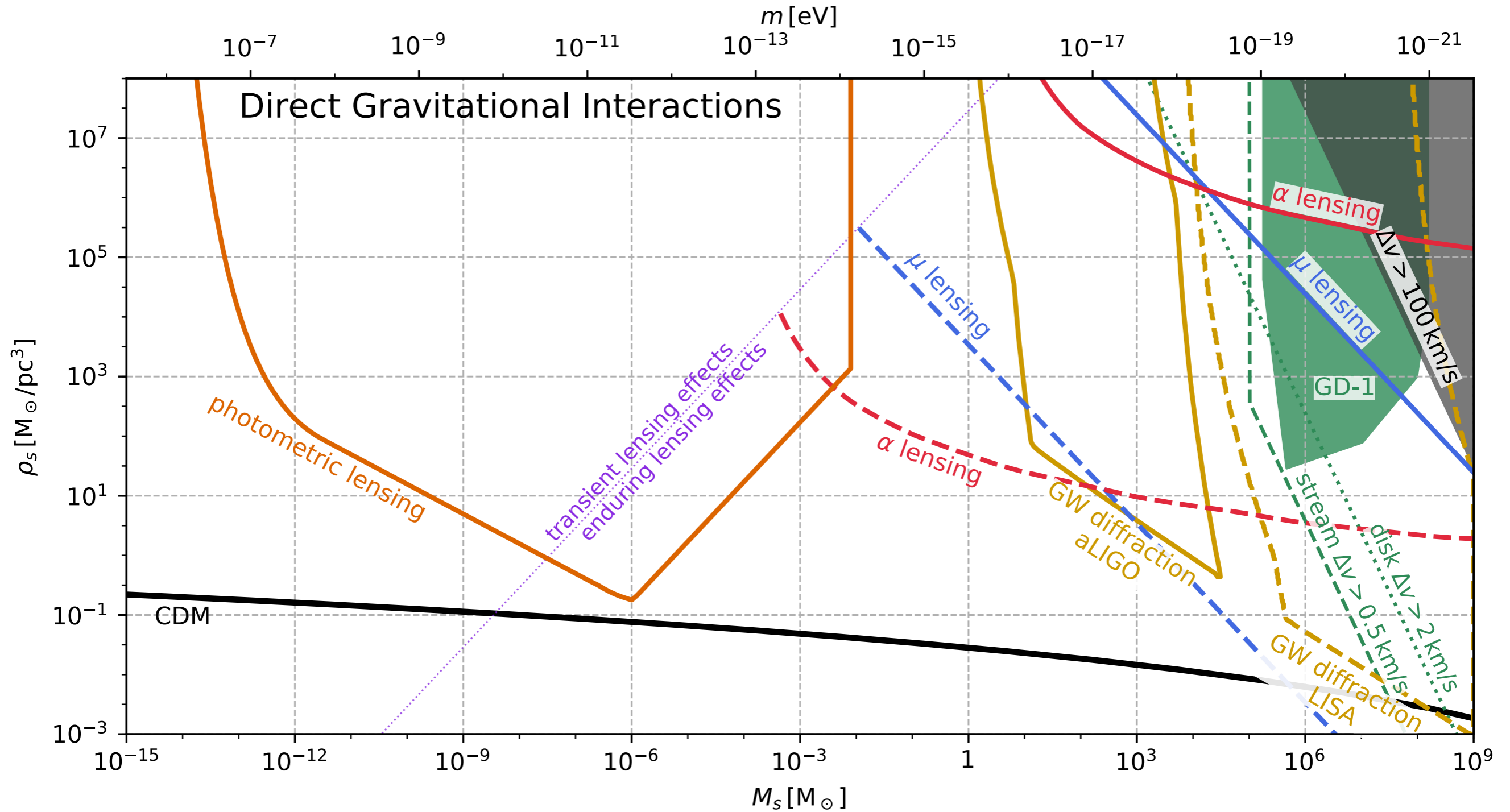
Dense Axion Halos & Solitons



QCD Axion

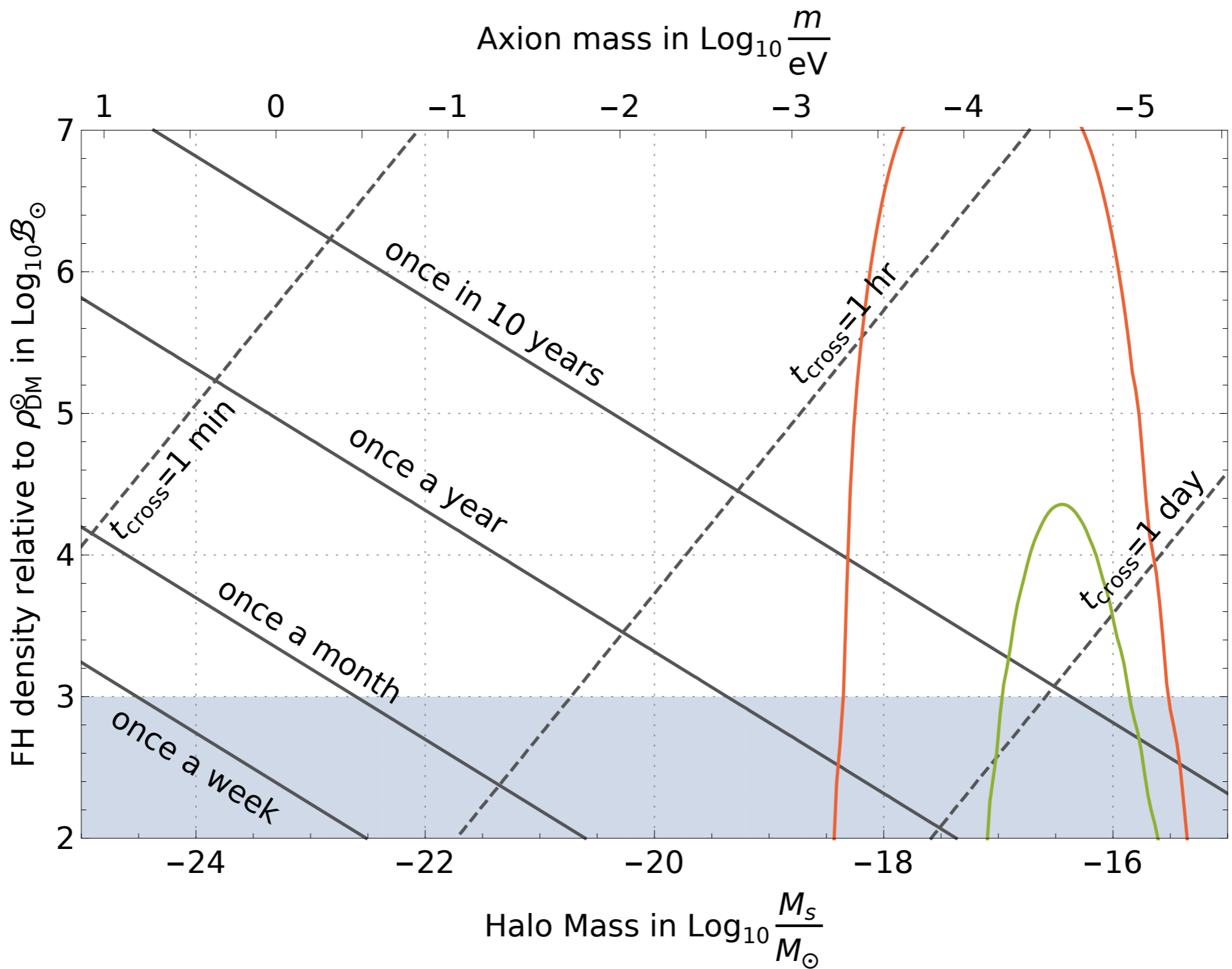


Gravitational Interactions



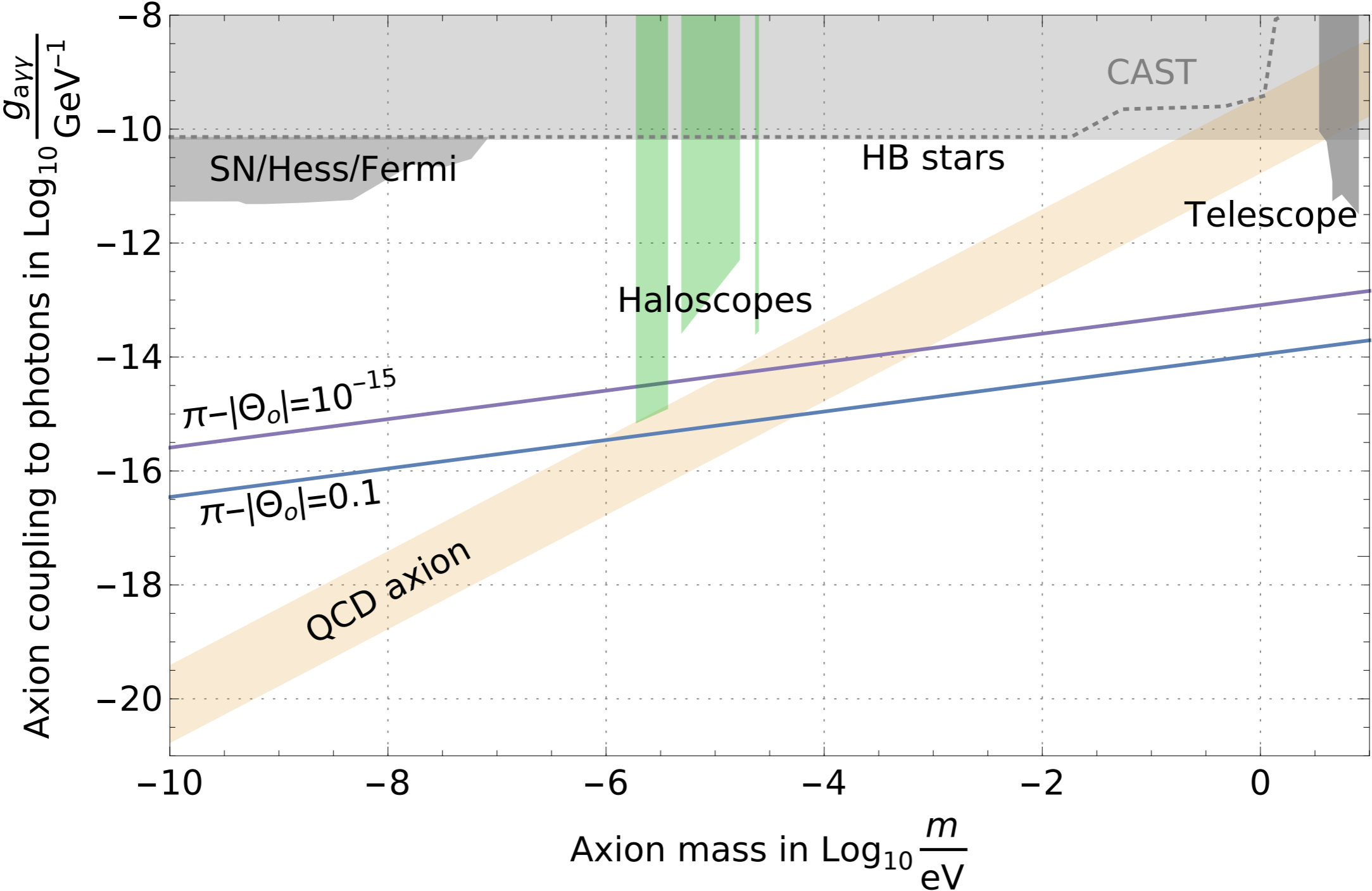
Direct Detection

intermittent, highly coherent signals \longrightarrow broadband data recording
matched filters



Direct Detection

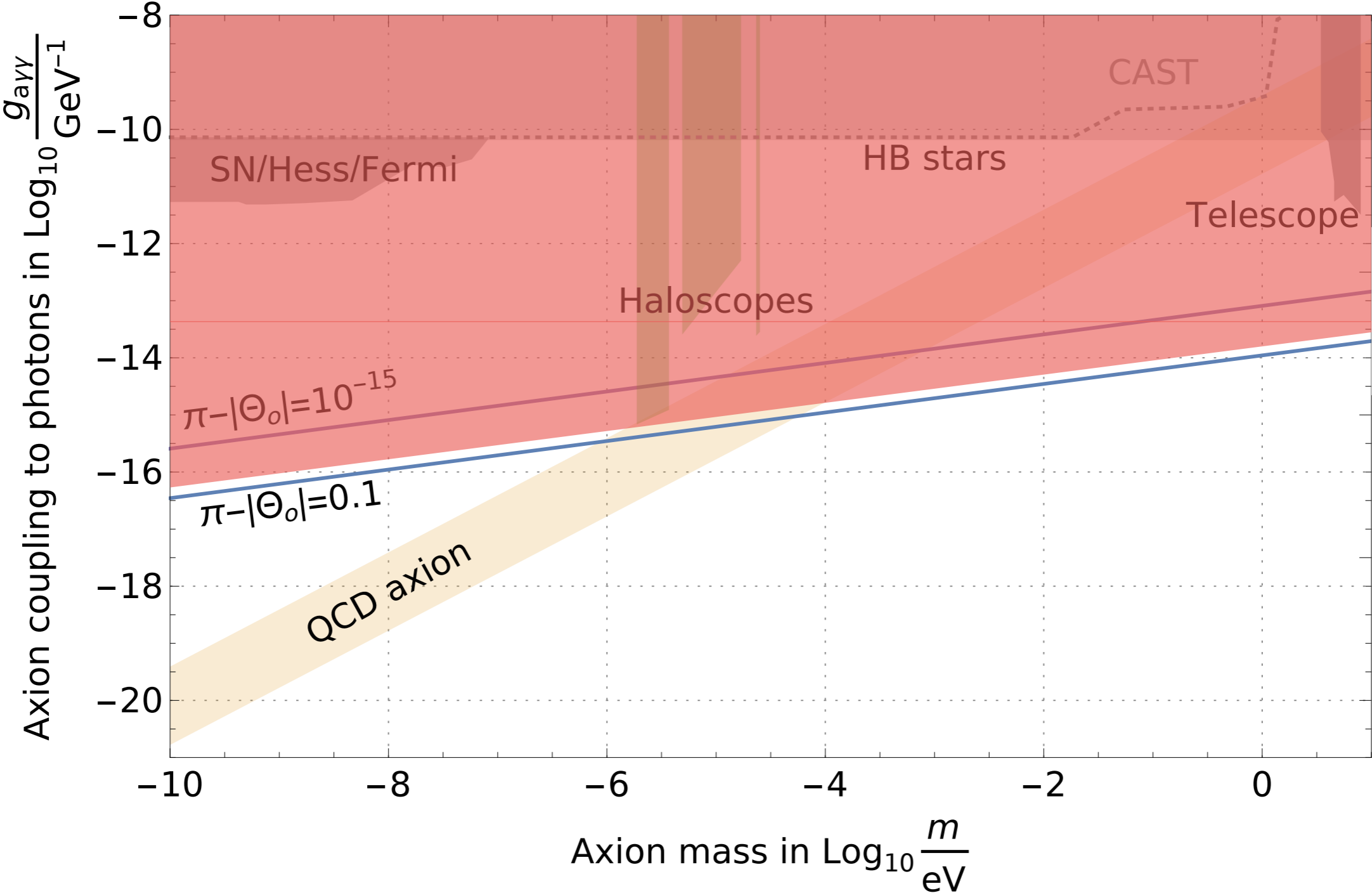
re-evaluate constraints and optimize high-frequency axion searches



[Michael's talk]

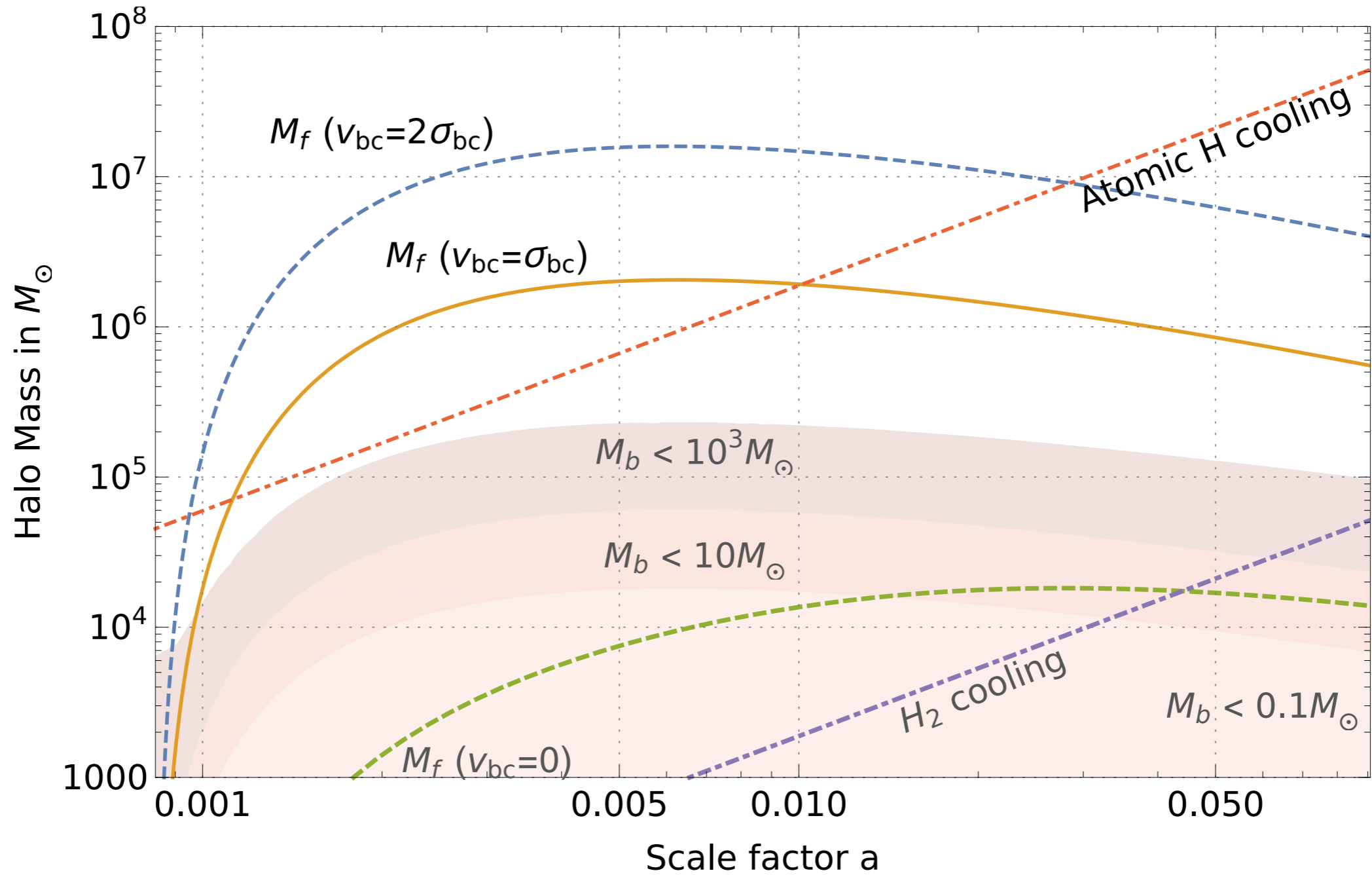
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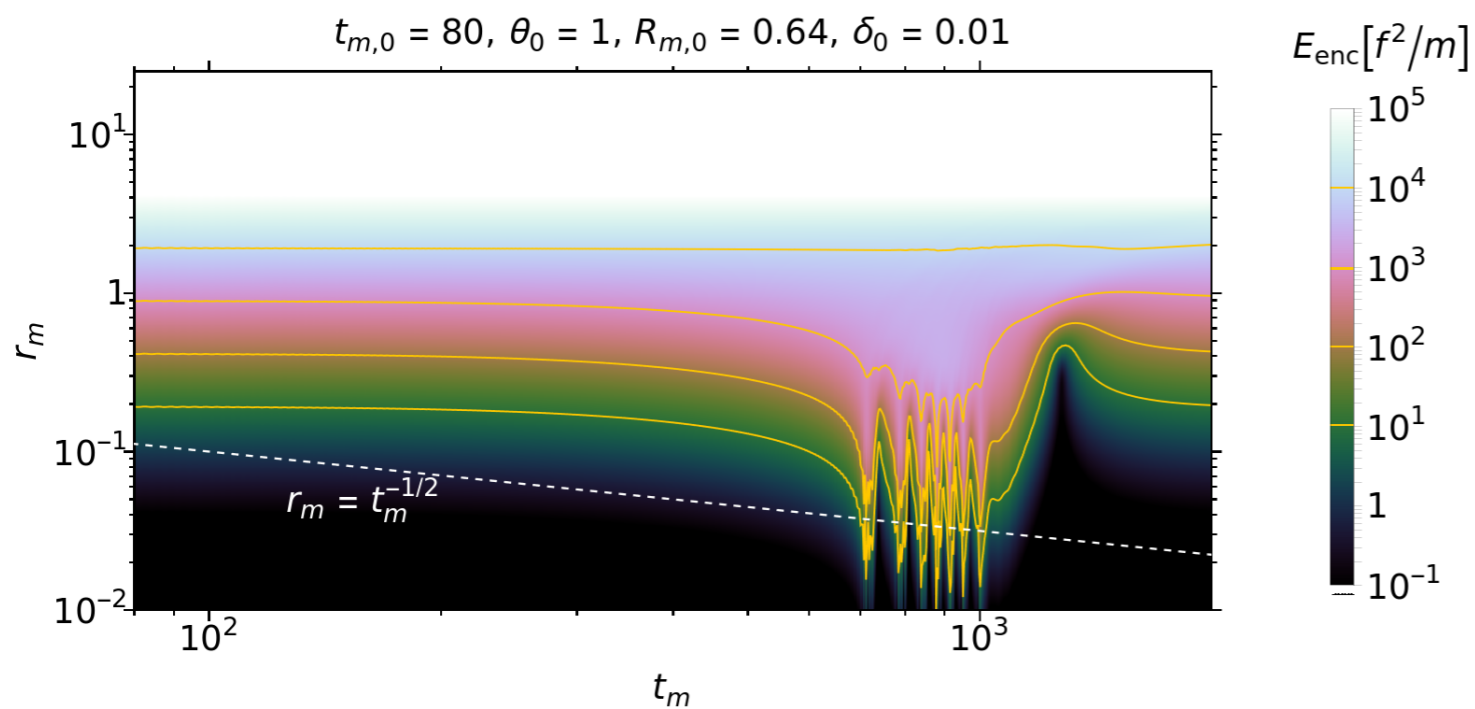
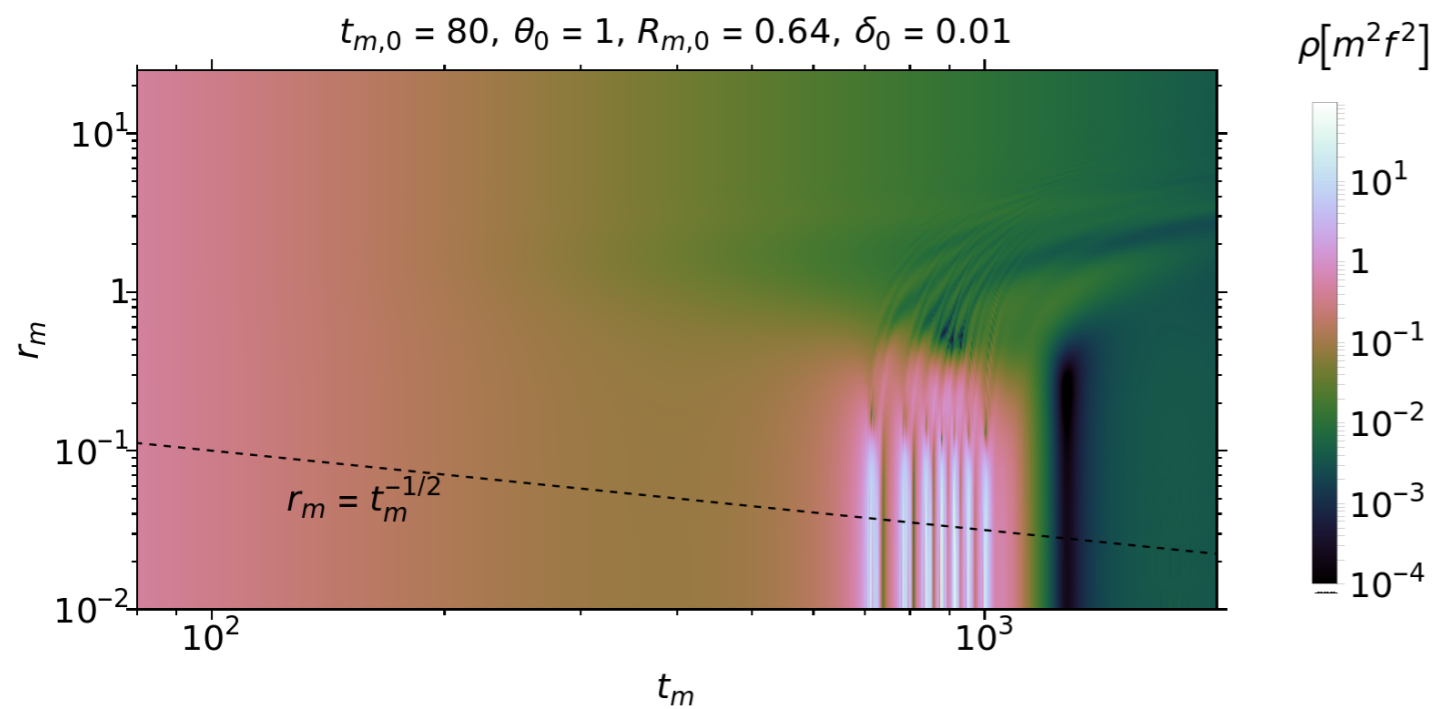


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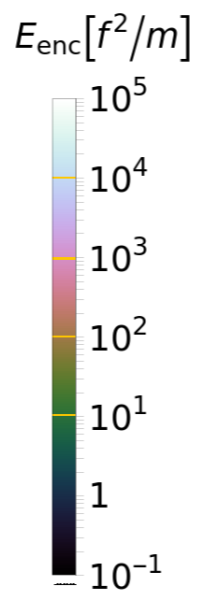
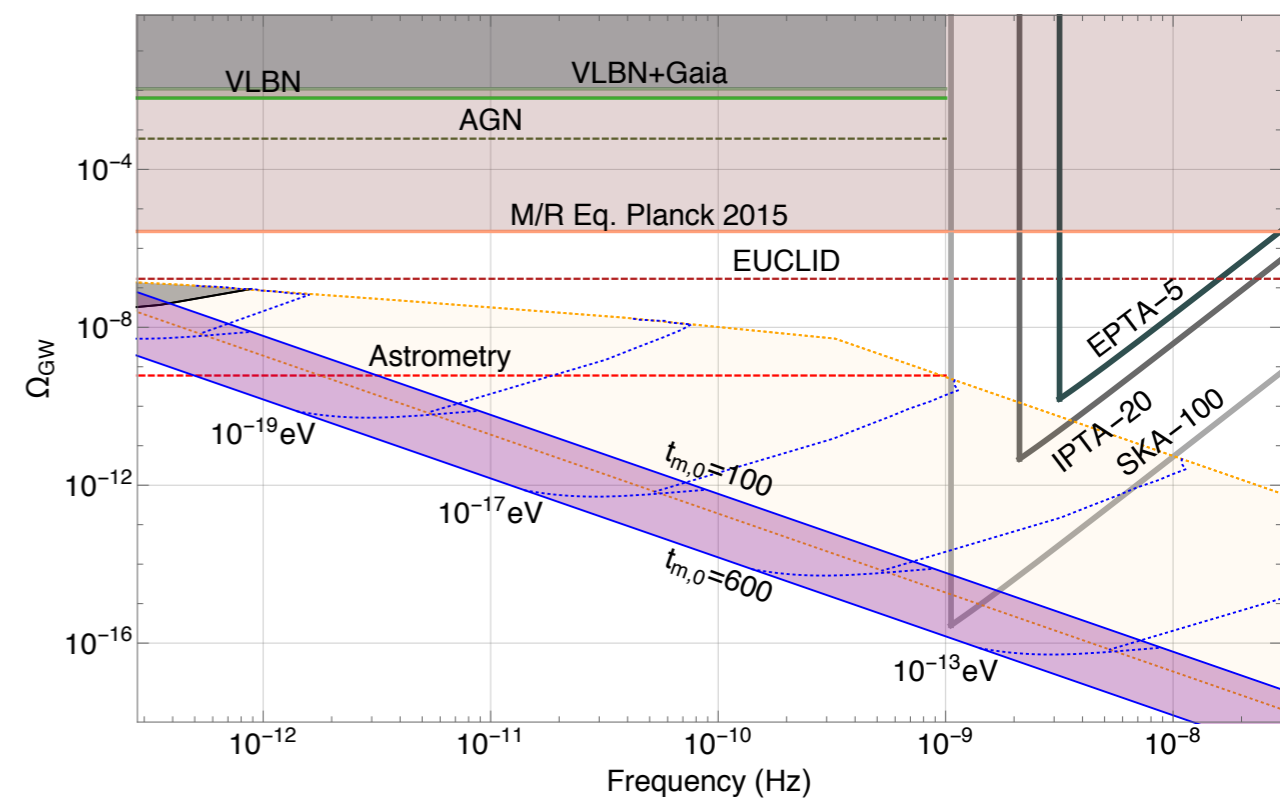
Baryonic Structure & Star Formation



Oscillon Production



Gravitational Waves

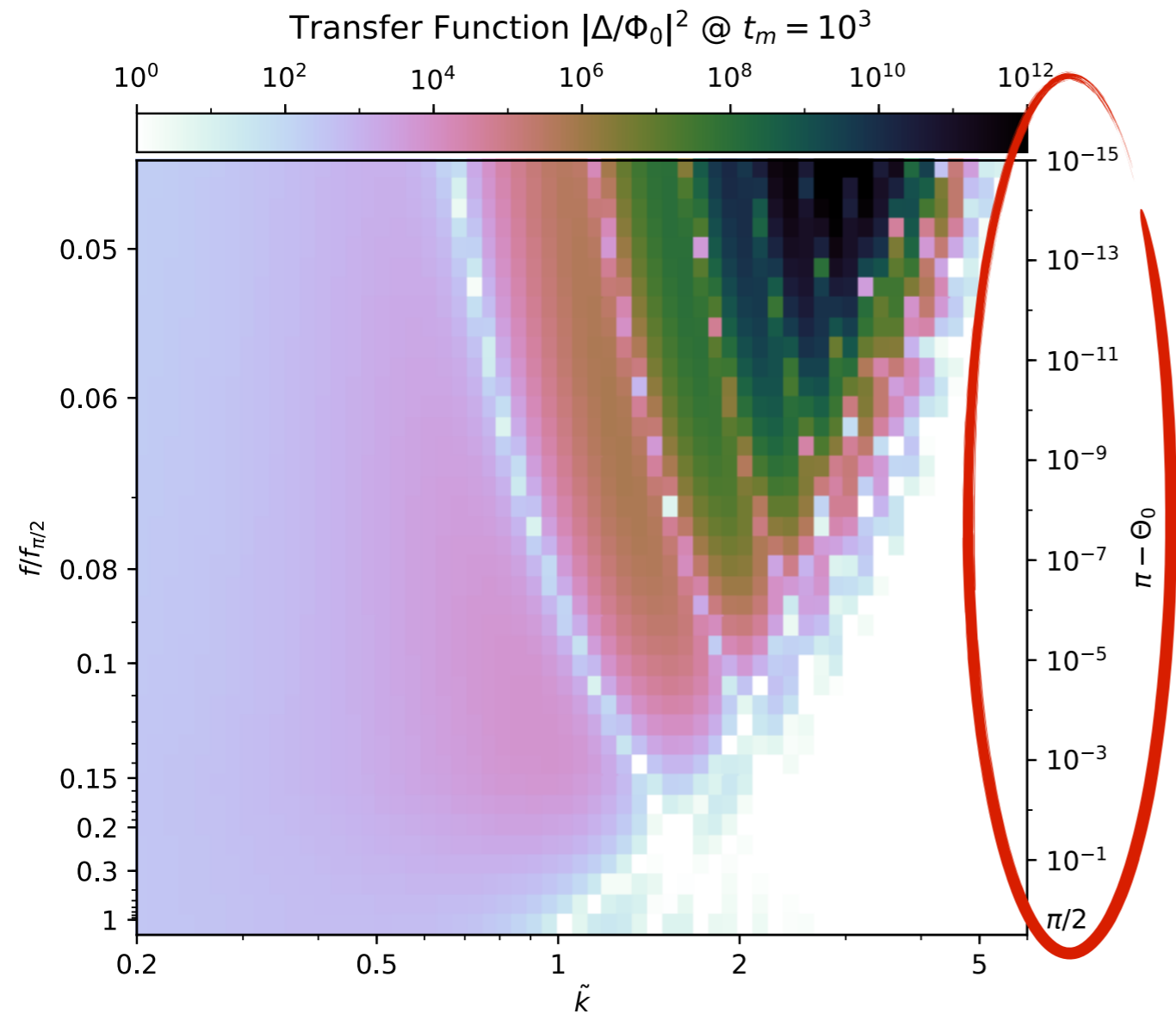


Initial Conditions

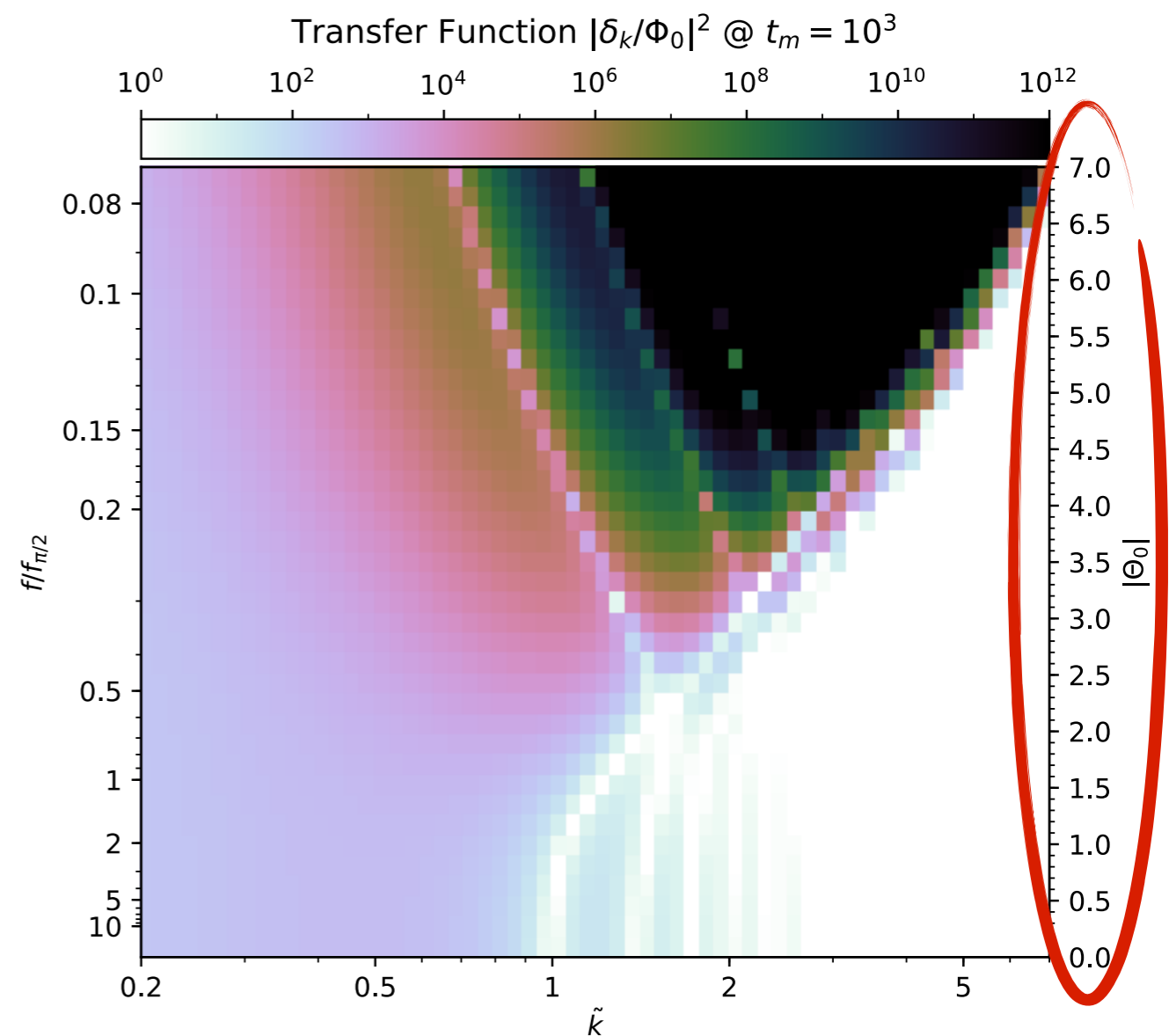
1. inflationary dynamics for $|\Theta_0| \simeq \pi$

2. environmental selection on DM abundance

3. large misalignment in other potentials:



$$V(\Theta) \propto (1 - \cos(\Theta))$$



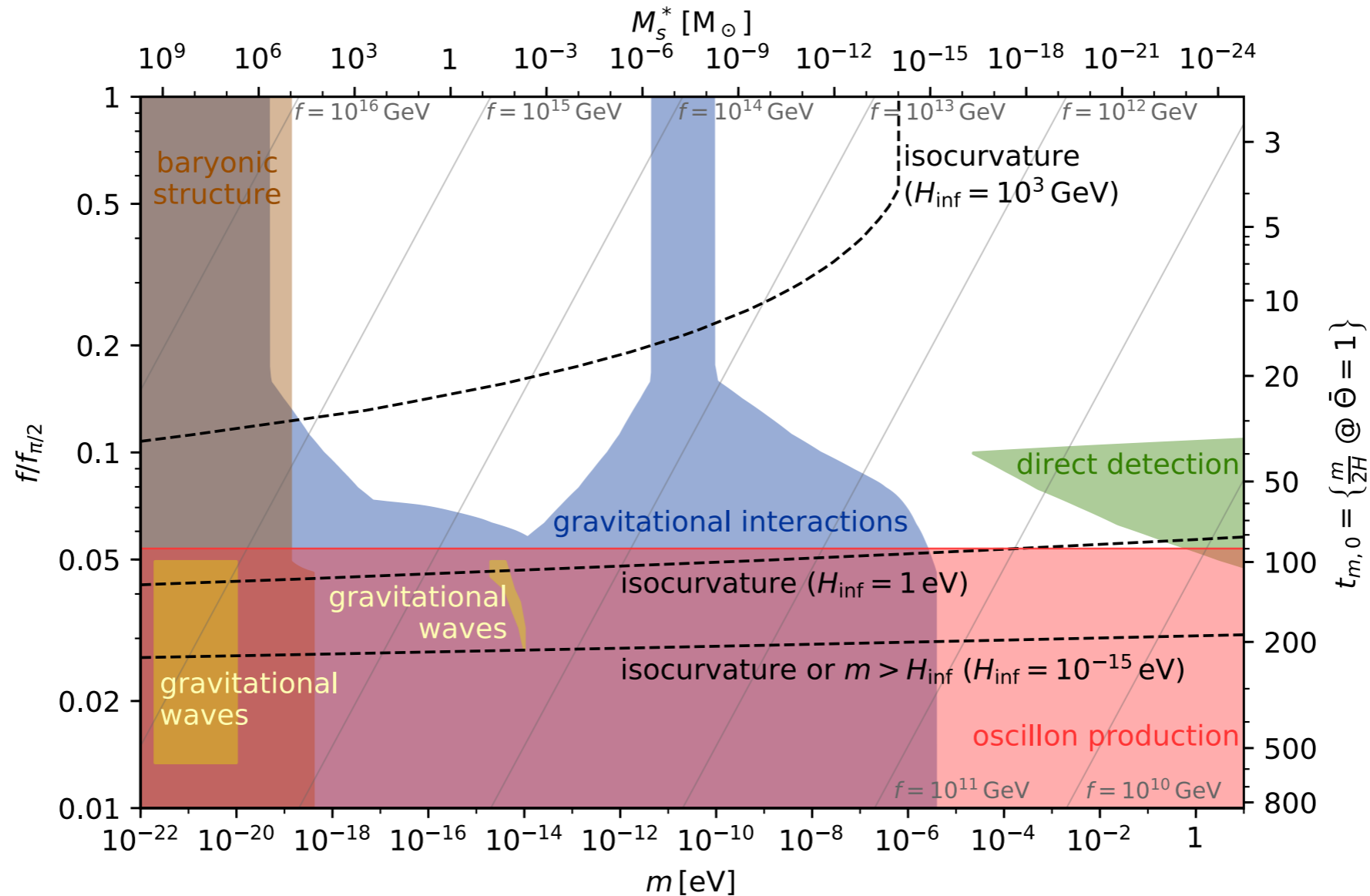
$$V(\Theta) \propto \frac{\Theta^2}{2 + \Theta^2}$$

Summary

If the onset of axion oscillations is delayed such that

$$\text{nonlinearities} > \text{Hubble friction, i.e. } \bar{\Theta}^2 \gtrsim \frac{4m}{H},$$

then semi-relativistic fluctuations grow exponentially to form compact axion structures

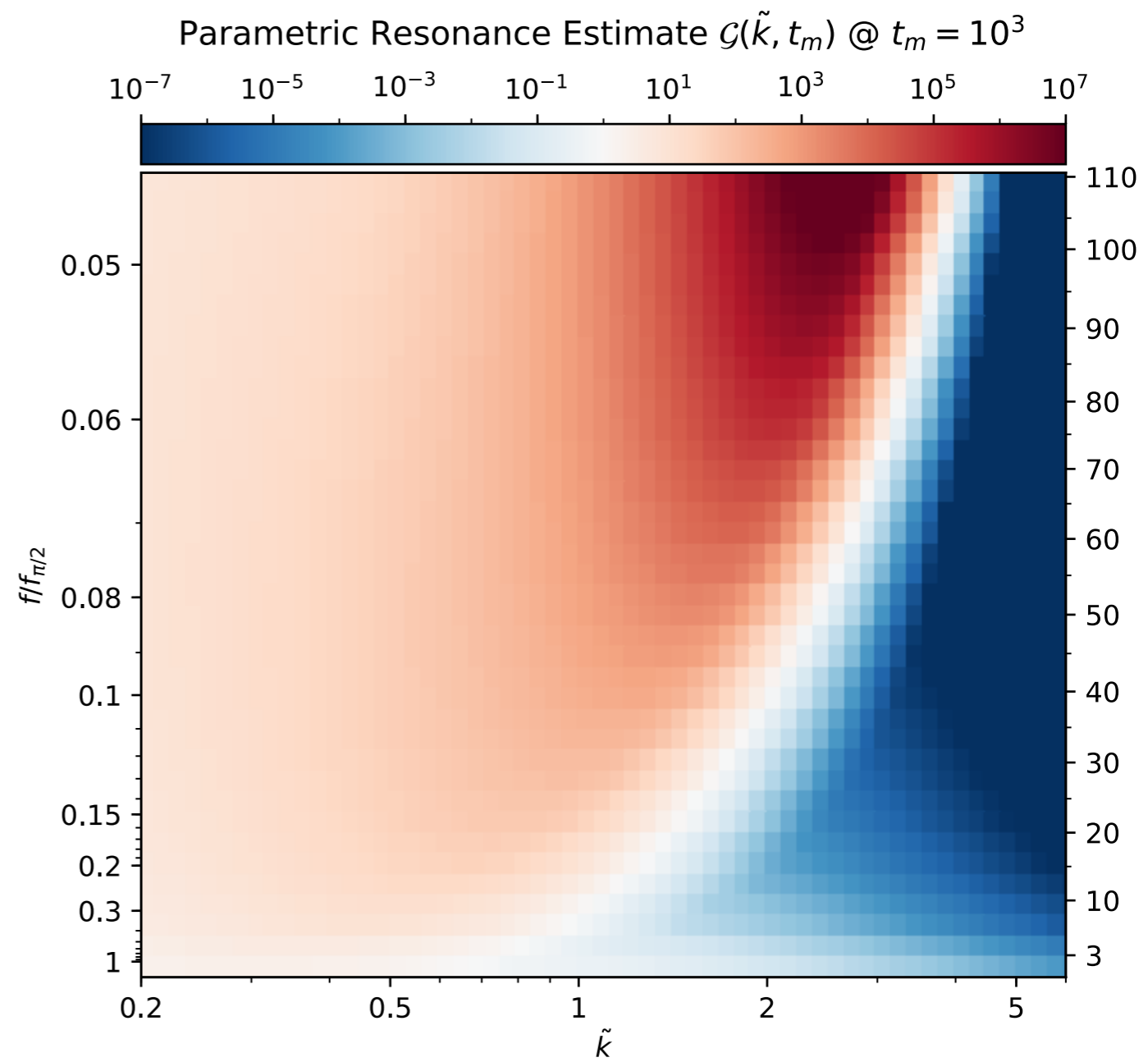
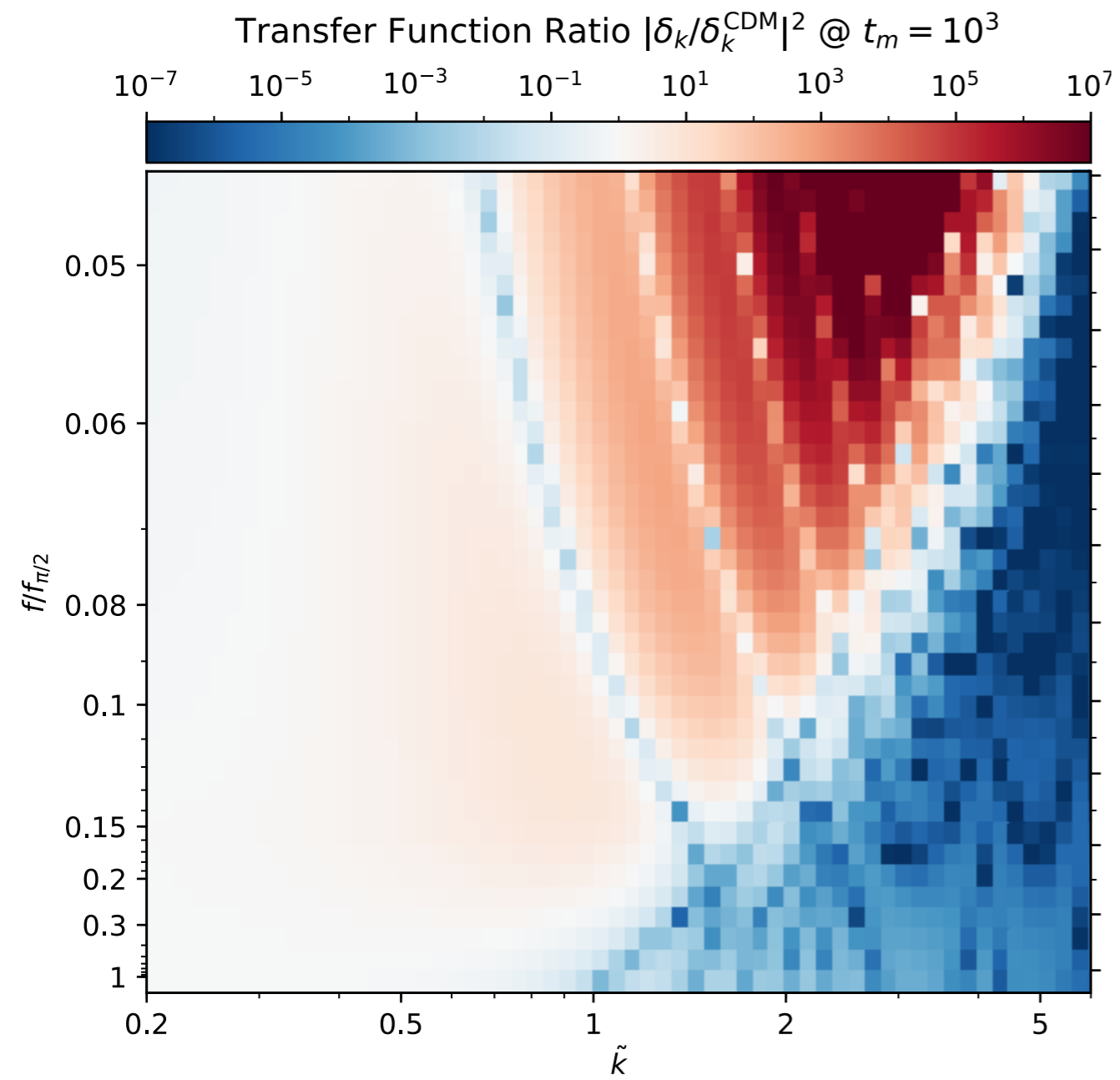


Open Questions:

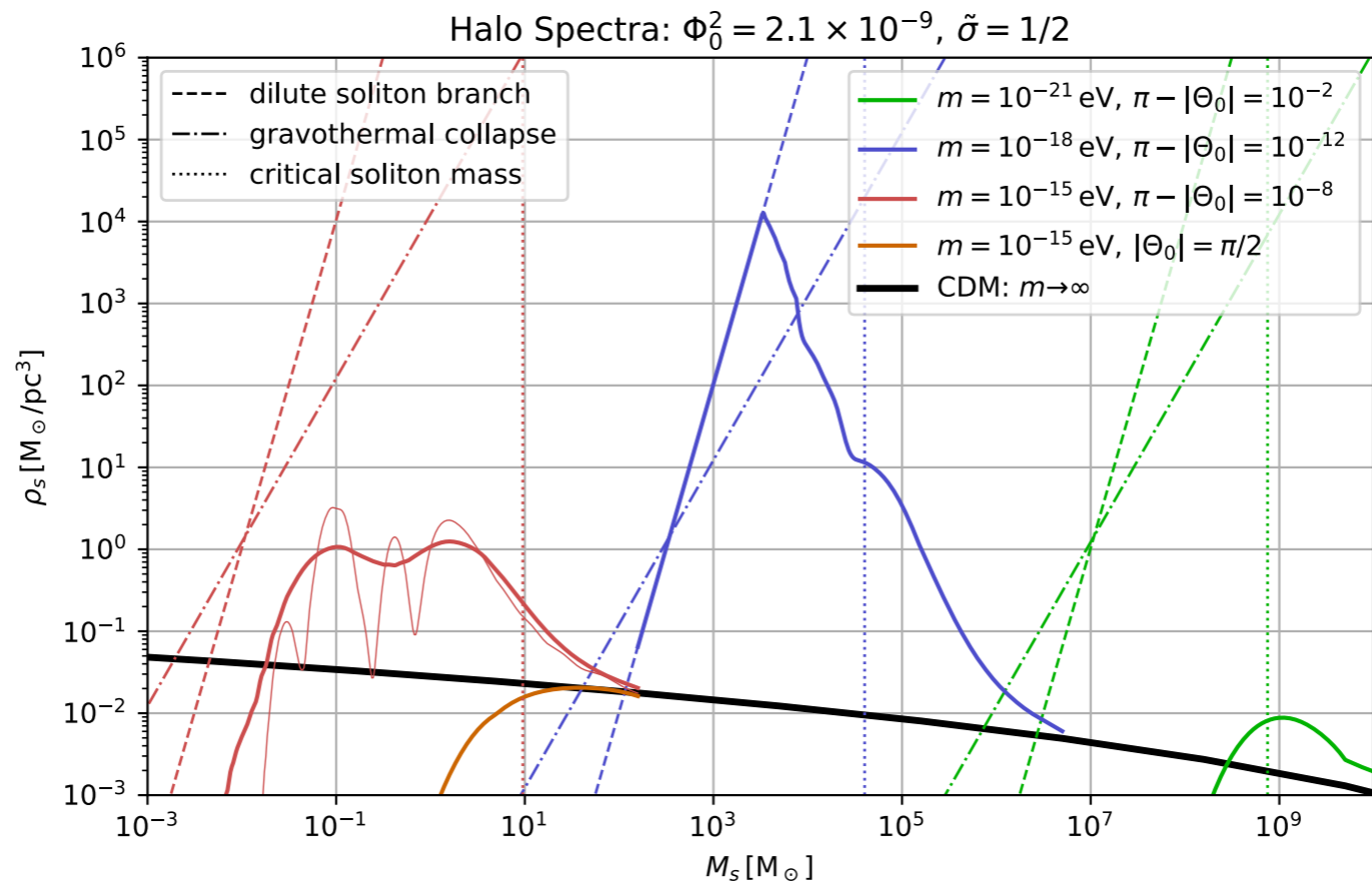
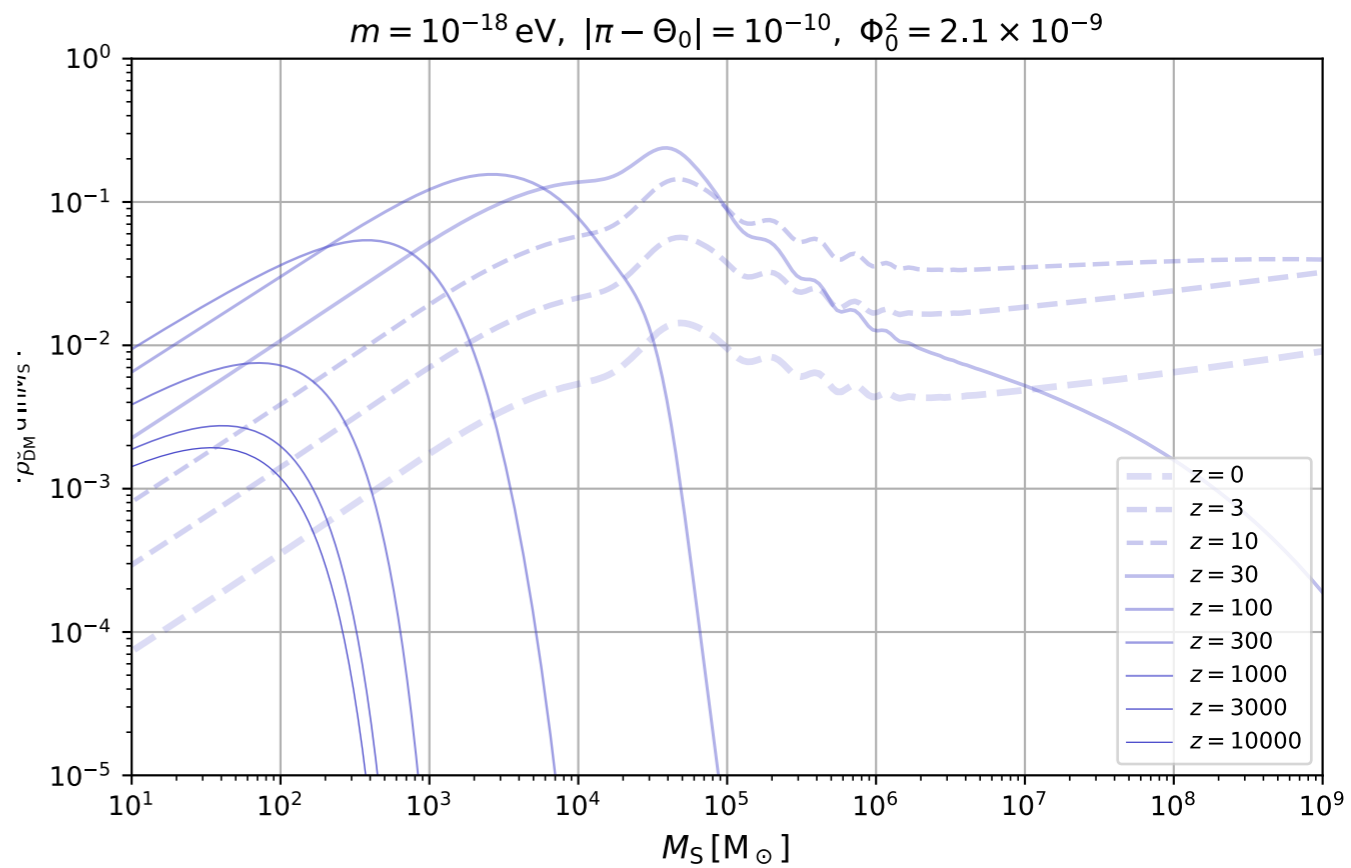
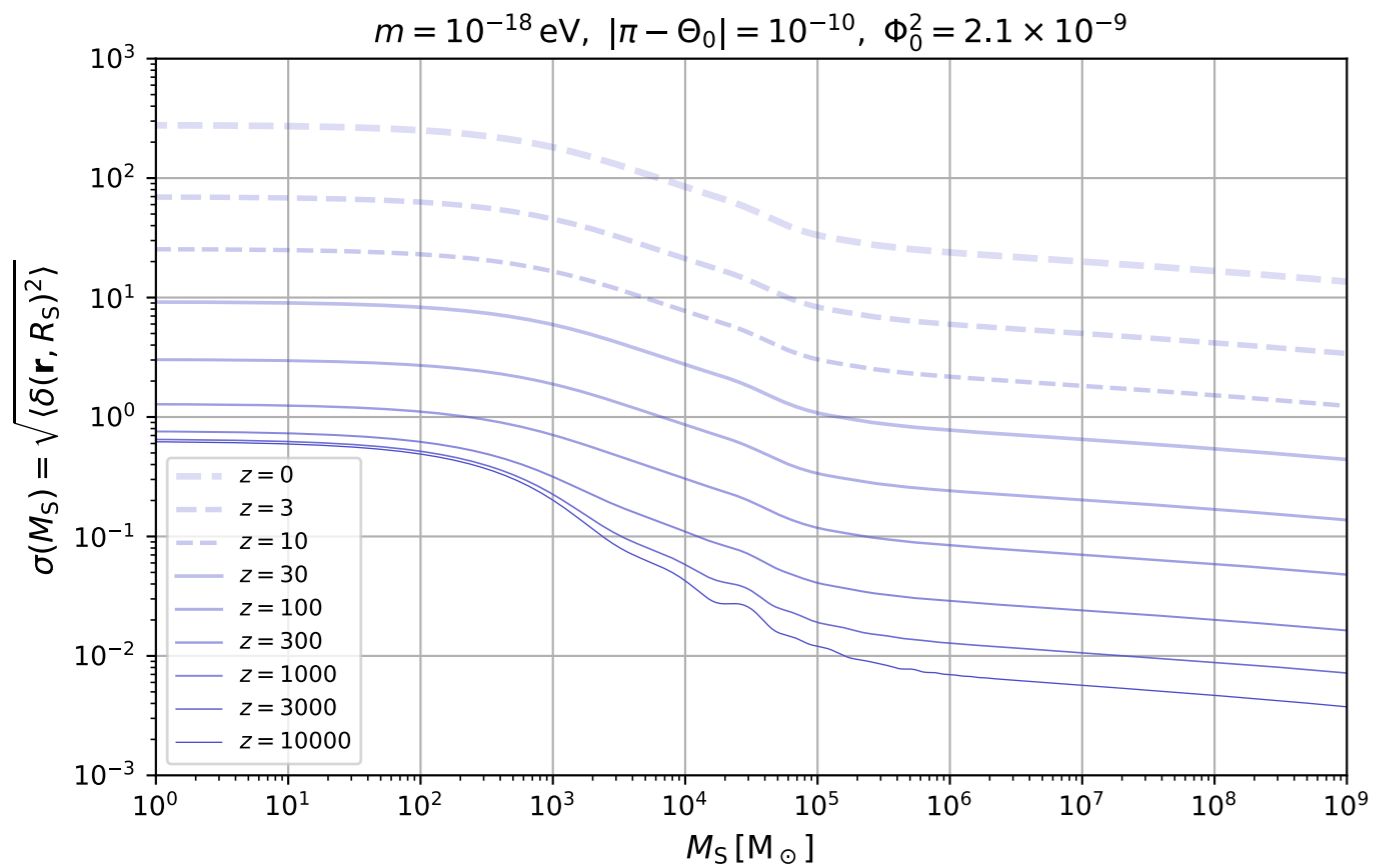
1. Nonlinear simulations:
 - tidal stripping
 - gravitational cooling
 - oscillon dynamics
 - GW production
2. Impact on direct detection
3. Star formation & re-ionization history
4. Analytic estimates of oscillon lifetime

Backup

Parametric resonance



Press-Schechter



Condition for Oscillon Formation

